

IM2 Problem Set 7.7 - Working with Quadratic Functions

BIG PICTURE
of this UNIT:

- How do we analyze and then work with a data set that shows both increase and decrease
- What is a parabola and what key features do they have that makes them useful in modeling applications
- How do I use graphs, data tables and algebra to analyze quadratic functions?
- How can I use graphs and equations of quadratic relations to make predictions from data sets & their models

1. (CI) Solve the following quadratic equations:

- | | | |
|----------------------------|---------------------------|------------------------------|
| a. (i) $x^2 - 4 = 0$ | (ii) $x^2 - 49 = 0$ | (iii) $3x^2 - 147 = 0$ |
| b. (i) $(x + 3)^2 - 4 = 0$ | (ii) $(x - 2)^2 - 49 = 0$ | (iii) $3(x - 5)^2 - 147 = 0$ |

2. (CI) Solve the following equations by first factoring the equation:

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|----------------------------|---------------------------|-----------------------------|
| a. (i) $x^2 - 4x - 32 = 0$ | (ii) $x^2 - 10x + 25 = 0$ | (iii) $x^2 - 6x = 0$ |
| b. (i) $2x^2 - x - 6 = 0$ | (ii) $9x^2 - 6x - 1 = 0$ | (iii) $3x^2 + 10x - 25 = 0$ |

3. (CA) Mr S throws a ball from the roof of a building which has a height of 25 m. The ball reaches a maximum height of 45 m two seconds later and hits the ground five seconds after being thrown.

- Draw an accurate sketch of the relation between the height of the ball and its time in flight.
- Where are the zeroes of the function?
- What are the coordinates of the vertex?
- Determine an equation that models this relationship?
- State the domain and range of the relation.

4. (CI)

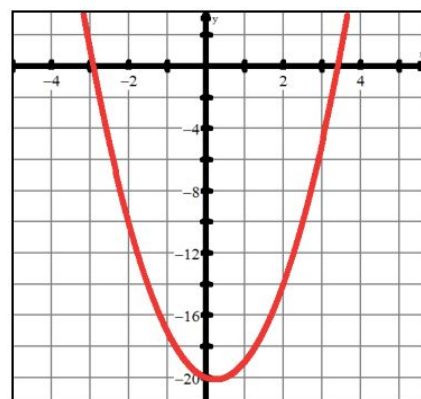
- One side of a rectangle is 4 m shorter than three times the other side. Find the sides if the perimeter of the rectangle is 48 m.
- One side of a rectangle is 4 m shorter than three times the other side. Find the sides if the area of the rectangle is 319 m^2 .

5. (CI) Find the intersection point(s) of the following functions. Then graph the two functions on your calculator to verify your answer(s).

- $f(x) = 5x + 7$ and $g(x) = x^2 + 2x + 3$
- $f(x) = -2x + 5$ and $g(x) = 10 + 2x - x^2$

6. (CA) Determine the equations of the parabolas from the information given in any form that is most convenient and then rewrite each equation in standard form.
- The function $h(x)$ has $h(-1) = h(11) = 0$ and the minimum value of $h(x)$ is -72 .
 - The function $g(x)$ has zeroes at $x = 4$ and $x = 9$ and $g(0) = -72$
 - The function $f(x)$ has an optimum point at $f(-2) = 12$ and a zero at $x = -4$.
7. (CI) The profits of a company in its first 13 months of operations are modeled by the quadratic function $P(m) = -\frac{1}{4}m^2 + 3m - 5$ where m is the number of months (and $m = 1$ represents January) and $P(m)$ is the profit measured in billions of Egyptian pounds.
- Evaluate $P(2)$ and interpret.
 - Determine the month in which the company maximizes its profits and what was the maximum profit?
 - Determine when the company breaks even and hence solve $P(m) < 0$.
 - State the domain and range of this profit function. Explain your reasoning.
 - Solve $P(m) = -12$ and explain why the profits might be negative.

8. (CA) Given the quadratic function $f(x) = 2x^2 - x - 20$ (graphed here), use the TI-84 to help you find necessary information and hence rewrite $f(x)$ in both factored form and vertex form.



EXTENSION PROBLEMS

9. The equation $ax^2 + 5x = 3$ has $x = 1$ as a solution. What is the other solution?
10. Find all x such that $\frac{10}{x^2} + \frac{22}{x} + 4 = 0$.
11. Find all solutions to $2w^4 - 5w^2 + 2 = 0$.
12. Find all solutions to the equation $\frac{x-6}{x-5} = \frac{4}{x-2}$.