## IM2 Problem Set 7.4 - Working with Quadratic Functions

BIG PICTURE of this UNIT:	<ul> <li>How do we analyze and then work with a data set that shows both increase and decrease</li> <li>What is a parabola and what key features do they have that makes them useful in modeling applications</li> <li>How do I use graphs, data tables and algebra to analyze quadratic functions?</li> <li>How can I use graphs and equations of quadratic relations to make predictions from data sets &amp; their models</li> </ul>
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- 1. (CA) Use your calculator to graph the following parabolas and then use the calculator to find the (i) vertex and (ii) the zeroes. Finally, rewrite each equation in *factored form* and in *vertex form*.
  - a.  $f(x) = x^2 2x 8$ b.  $g(x) = 2x^2 - 4x$ c.  $h(x) = 3x^2 + 9x - 30$
- 2. (CI) Given the pattern .....24, 21, 16, 9, 0, -11, -24, ....
  - a. How do you know the pattern is NOT linear?
  - b. How do you know the pattern is NOT exponential?
  - c. What are the next three terms of the sequence
  - d. What are the 3 terms that came **before** 24?
- 3. (CI) Using this pattern from Q2 (.....24, 21, 16, 9, 0, -11, -24, ....), we create the following data set:

x	4	5	6	7	8	9	10
f(x)	24	21	16	9	0	-11	-24

- a. At which *x* coordinate will the second *x*-intercept be?
- b. Find the vertex of the parabola.
- c. Using the two forms of the quadratic equations, write equations for this quadratic function.
- d. Evaluate the following: f(11), f(12), f(13), and f(14)
- e. Hence, evaluate the following:
  - i. (i) [f(14) f(13)] [f(13) f(12)]
  - ii. (ii) [f(13)-f(12)] [f(12) f(11)]
  - iii. Explain your observations in these calculations
- 4. (CI) Use distribution to simplify the following products:

a. (i) 
$$(r+1)(r-3)$$
 (ii)  $(k-2)(k-3)$  (iii)  $(g-5)^2$  (iv)  $(2x-1)^2$   
b. (i)  $(3p-3)(p-1)$  (ii)  $(2x-3)(3x+3)$  (iii)  $(4n+4)(5n-8)$ 

- 5. (CI) Two parabolas have zeros of 1 and 11. One has a maximum value of 12 and the other has a minimum value of -6. Sketch the two parabolas on the same axes and then determine their equations.
- 6. (CA) A penguin dives into a lake to catch a fish. The underwater path of the penguin is described by the model  $d(x) = \frac{1}{2}x^2 3x$ , where x represents the horizontal position of the penguin relative to its entry point and d is the depth of the penguin underwater. Both measurements are in meters.
  - a. Graph the parabola on your calculator. State your window settings.
  - b. Explain what the point (2, -4) represents in the context of this problem.
  - c. State the domain and range in the context of this problem.
  - d. What is the greatest depth below the water surface?
  - e. Factor the equation  $y = \frac{1}{2}x^2 3x$ .
- 7. (CI) The vertex of a parabola is at (4,-2) and the parabola goes through the point (0,6). Determine:
  - a. if the relation has a maximum or minimum value?
  - b. the equation of the quadratic relation.
  - c. the coordinates of the *x*-intercepts.
  - d. Sketch the parabola.
- 8. (CI) The following quadratic functions are written in standard form ( $y = ax^2 + bx + c$ ). Rewrite the following equations in factored form. The process you are carrying out is called *factoring*.
  - a. (i)  $y = x^2 x 6$  (ii)  $y = x^2 + x 12$  (iii)  $y = x^2 + 5x + 4$  (iv)  $y = x^2 4x 32$ b. (i)  $y = 2x^2 - 2x - 12$  (ii)  $y = 3x^2 + 24x + 45$
  - b. (1)  $y = 2x^2 2x 12$  (11)  $y = 3x^2 + 24x + 45$
- 9. (CA) A company models the profit of its latest video game using the relation  $P(x) = -4x^2 + 20x 9$ , where *x* is the number of games produced (in hundreds of thousands) and *P* is the profit in millions of dollars.
  - a. Explain what the point (5,-9) means in the context of this problem.
  - b. Suggest a reasonable domain for this relation, given the context of the problem.
  - c. What are the break even points for the company?
  - d. What is the maximum profit that the company can earn?
  - e. How many games must be produced to earn this maximum profit?
  - f. Rewrite the equation in vertex form.

## **EXTENSION PROBLEMS**

- 10. Write the product of two binomials such that the product is equal to zero when x = 3 and x = -5.
- 11. 100 times my number is equal to the square of my number divided by 4. What are the possible values of my number?
- 12. The sum of the roots of a quadratic equation is equal to -3, while the product of the roots is -40. Find the equation of this quadratic as well as finding the values of the two roots.