

## IM2 Problem Set 5.4 - Linear Functions

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BIG PICTURE of this UNIT:	<ul style="list-style-type: none"><li>• What is meant by the term FUNCTIONS and how do we work with them?</li><li>• mastery with working with basics &amp; applications of linear functions</li><li>• mastery with working with basics &amp; applications of linear systems</li><li>• understanding basics of function concepts and apply them to lines &amp; linear systems</li></ul>
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### Part 1 - Skills/Concepts Review

1. A relation is defined by the following description: *To “create/generate” a new value, a number is doubled and then increased by four.* The CONDITION on the “starting” number is that it must be a real number between and including 0 and 10.
  - a. Use the starting numbers of  $x = 0, 1, 2, 3, \dots, 8, 9, 10$  to create a table of values for this relation.
  - b. List 3 ordered pairs for this relation.
  - c. Create an equation for this relation.
  - d. Graph this relation. What are the domain and range for this relation?
2. For the linear function defined by  $2x - 8y - 32$ , determine
  - a. the range of this function if the domain is  $\{-2 < x \leq 4\}$ .
  - b. the domain of this function if the range is  $\{-12 \leq y < 4\}$
  - c. where this function intersects the function  $f(x) = \frac{1}{4}x + 6$
3. A corn plant grows at an average rate of 4.5 mm/day from the start of the third week to the end of the sixth week. During this time period, the plant’s growth can be modeled by  $h(d) = 4.5d + 25$ , where  $h$  is the plant’s height in mm and  $d$  is the number of days since the beginning of the third week.
  - a. What do the numbers 4.5 and 25 represent?
  - b. What domain has been given in this question?
  - c. What is the range of this function?
4. Determine the equation of a line that is:
  - a. parallel to  $3x + 2y - 9 = 0$  and passes through  $(-2, 5)$ . Sketch this line.
  - b. parallel to the  $x$ -axis and goes through the point  $(-2, 5)$ . Sketch this line.
  - c. parallel to the  $y$ -axis and goes through the point  $(-2, 5)$ . Sketch this line.

## **Part 2 - Skills/Concepts Application Problems**

5. Given the lines defined by  $-6x + 2y = -4$  and  $y = -3x + 1$ :
- Use your calculator to determine the intersection point.
  - Now, use the substitution method to algebraically find the point where the lines  $-6x + 2y = -4$  and  $y = -3x + 1$  intersect.
6. Mr. S has \$18,000 savings in 2 investment accounts. Last year, he earned a total of \$930 of interest from these 2 accounts. One of the accounts earns 6% annual interest and the other account earns 3% annual interest.
- Why would Mr S invest his money in 2 different accounts in the first place?
  - One equation that Mr S writes to model this problem is  $0.06x + 0.03y = 930$ . Explain
    - what the variables  $x$  and  $y$  represent
    - what  $0.06x$  represents
  - The second equation Mr S writes is  $x + y = 18000$ . Explain why.
  - How much does Mr S have invested in each account?
7. Solve the linear system  $y = 2x - 4$  and  $3x + 2y = 15$  using the substitution method.
8. Next week, your math teacher will give you a test worth 100 points. The test will consist of 35 problems, some of which are worth 2 points and some problems are worth 4 points. How many 2 mark and how many 4 mark questions are on the test?
- Since there are 2 unknowns in this problem, we need to write 2 equations that model the relationships involving our unknowns. One equation that Mr R proposes is  $x + y = 35$ . Explain why this equation is correct.
  - What might the variables  $x$  and  $y$  represent?
  - Write a second equation that shows how the two unknowns are related.
  - Solve this system of equations.
  - How many 2 mark and how many 4 mark questions are on the test?
9. Determine the value of the unknown in the following problems:
- Find  $A$  if the graph of the equation  $Ax + 3y = 5$  is parallel to the graph of  $5x - 2y = 4$
  - Find  $B$  if the graph of the equation  $3x = By + 2$  is perpendicular to the graph of  $3y = -2x + 4$
  - Find  $A$  and  $B$  if the graph of  $Ax + 3y = B$  produces the same line as the graph of  $2x + 6y = 7$

10. Let  $f(x) = 2x - 6$  and let  $g(x) = 3x - 9$ .

- a. Evaluate (i)  $f(-3)$       (ii)  $f(4) - f(3)$       (iii)  $f(5) - f(4)$       (iv)  $f(A + 1) - f(A)$
- b. Evaluate (i)  $f(g(2))$       (ii)  $g(f(2))$

11. The Yearbook club is considering two different companies to print this year's yearbook. The Descartes Publishing Co. charges a flat fee of \$475 plus \$4.50 per book. The Euclidean Publishing Co. charges a one time fee of \$550 plus \$4.25 per book.

- a. Each of the company's costs to publish the yearbooks can be modeled using linear equations. Write two equations to model the publishing costs.
- b. Which company should our Yearbook club use? Why.

12. Given the equation  $5x - 2y - 29 = 0$ ;

- a. change the equation  $5x - 2y - 29 = 0$  into slope-intercept form as well as slope-point form.
- b. determine the point on the line  $5x - 2y - 29 = 0$  that is closest to the origin.

### Part 3 - Extension Problems

13. A line with a slope of 3 intersects a line with a slope of 5 at the point (10,15). What is the distance between the  $x$ -intercepts of these 2 lines?

14. Let  $f(x) = 2x - 6$  and let  $g(x) = 3x - 9$ .

- a. Find  $f(g(2))$  as well as  $g(f(2))$  as well as  $f(g(x))$ .
- b. Let  $h(x) = 3x + 10$ . For what value of  $x$  does  $h(h(x)) = x$ ?