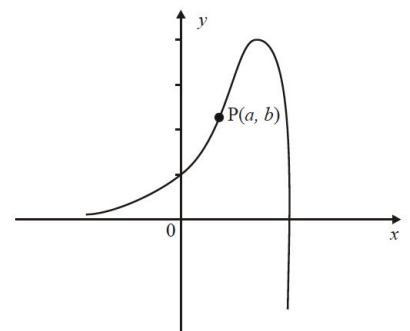


1. (CI) Find the equation of the tangent to the curve  $y = e^{2x}$  at the point where  $x = 1$ . Give your answer in terms of  $e$ .
  
2. (CI) Let  $f(x) = 3 \cos(2x) + \sin^2(x)$ .
  - a. Show that  $f'(x) = -5 \sin(2x)$
  - b. In the interval  $\frac{\pi}{4} \leq x \leq \frac{3\pi}{4}$ , one normal to the graph of  $f$  has an equation  $x = k$ . Find the value of  $k$ .
  
3. (CA) Let  $f(x) = \cos(2x)$  and let  $g(x) = \ln(3x - 5)$  and let  $h(x) = f(x) \times g(x)$ .
  - a. Explain why the domain of  $h(x)$  is  $x > \frac{5}{3}$ .
  - b. Determine the equation of  $h'(x)$ .
  - c. Hence, or otherwise, determine the intervals in which  $h(x)$  is concave down. Include explanations of how you used the calculator to determine your domain interval.
  
4. (CI) Consider the function  $f(x) = k \sin(x) + 3x$ , where  $k$  is a constant.
  - a. Find  $f'(x)$ .
  - b. When  $x = \frac{\pi}{3}$ , the gradient of the curve of  $f(x)$  is 8. Find the value of  $k$ .
  
5. (CI) Consider the curve  $y = \ln(3x - 1)$ . Let  $P$  be a point on the curve where  $x = 2$ .
  - a. Find the gradient of the curve at  $P$ .
  - b. The normal to the curve at  $P$  cuts the  $x$ -axis at  $R$ . Find the coordinates of  $R$ .
  
6. (CI) Let  $g(x) = 2x \sin(x)$ . Find the gradient of the curve at  $x = \pi$ .
  
7. (CI) Find the exact value of  $h'(\frac{\pi}{3})$  if  $h(x) = e^{-3x} \sin(x - \frac{\pi}{3})$ .
  
8. (CI) The diagram shows part of the graph of the curve with equation  $y = e^{2x} \cos x$ .
  - a. Show that  $\frac{dy}{dx} = e^{2x}(2 \cos(x) - \sin(x))$ .
  - b. Hence, find  $\frac{d^2y}{dx^2}$  (the second derivative).

There is an inflexion point at  $P(a, b)$ .



- c. Use your results from parts (a) and (b) to prove that:
  - i.  $\tan(a) = \frac{3}{4}$ ,
  - ii. the gradient of the curve at  $P$  is  $e^{2a}$ .