

1. **(CI)** Determine the equations of the derivatives of the following functions.

- a. $y = x \ln(x)$
- b. $y = \frac{4}{x^2} \sin(x)$
- c. $y = 2x^3 e^{-x}$
- d. $y = x^3 \cos(x)$
- e. $y = e^{3x} \cos(x)$
- f. $y = -\frac{\sqrt{x}}{5} \ln(x)$

2. **(CI)** Determine the equations of the lines *tangent* to the following functions at the specified points.

- a. $g(x) = xe^{1+x^2}$ at the point where $x = 0$.
- b. $h(x) = x^2 \cos(x)$ at the point where $x = \pi$.
- c. $f(x) = \frac{1}{x} \ln(x)$ at the point where $x = e$.

3. **(CA)** Determine the equations of the lines *normal* to the following functions at the specified points.

- a. $g(x) = xe^{1+x^2}$ at the point where $x = \frac{1}{2}$.
- b. $h(x) = x^2 \cos(x)$ at the point where $x = \frac{1}{4}$.
- c. $f(x) = \frac{1}{x} \ln(x)$ at the point where $x = e^2$.

4. **(CI)** For the curve of $g(x) = e^x \sin(x)$ on the domain of $-\pi \leq x \leq \pi$,

- a. Show that $g(x)$ has 2 zeroes at $x = -\pi$ and $x = 0$ and $x = \pi$.
- b. Find the equations of $g'(x)$ and $g''(x)$.
- c. Find the values of x for which $g'(x) = 0$.
- d. Hence, determine the interval(s) of increase and decrease of $g(x)$ and classify the extrema.
- e. Sketch the function, given your previous work.

5. **(CI)** Given the function $g(x) = xe^x - e^x$,

- a. Find the exact values of $g(1)$ and $g(0)$.
 - b. Show that $\frac{d}{dx} g(x) = e^x + g(x)$.
 - c. Determine the intervals of increase and decrease for $y = g(x)$.
 - d. Show that $g(x)$ has an inflection point at $x = -1$.
 - e. Determine the interval in which $g(x)$ is concave up.
 - f. Sketch the function given your previous work.
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