

1. **(C5.4 - N) (CI)** Determine the equations of the specified lines that are *tangent* and *normal* to the following functions at the specified points. (Reminder: a **normal line** is perpendicular to a **tangent line**)

(Cirrito 20.1, p.646)

- $g(x) = x^2(2x - 1)(x + 3)$ at the point where $x = -1$.
- $f(x) = 2\sqrt{x} - \frac{1}{2}x$ at the point where $x = 4$.
- $h(x) = \frac{2}{x} - \frac{2}{x^2}$ at the point where $x = -1$.

2. **(C5.4 - N) (CA)** At what x value(s) does the curve $y = \frac{1}{2}x^4 + \frac{4}{3}x^3 - x^2 - 6x + 7$ have a tangent line that is perpendicular to the line $2y - x + 6 = 0$?

(Cirrito 20.1, p.646)

3. **(C5.4 - N) (CI)** The tangent line to a curve $y = f(x)$ at $x = 2$ passes through the points $(0, -20)$ and $(5, 40)$. What are the values of $f(2)$ and $f'(2)$?

(Cirrito 20.1, p.646)

4. **(C5.4 - N) (CI)** The tangent line to a curve $y = f(x)$ at $x = 1$ passes through the point $(4, 9)$. If $f(1) = 3$, then what is the value of $f'(1)$?

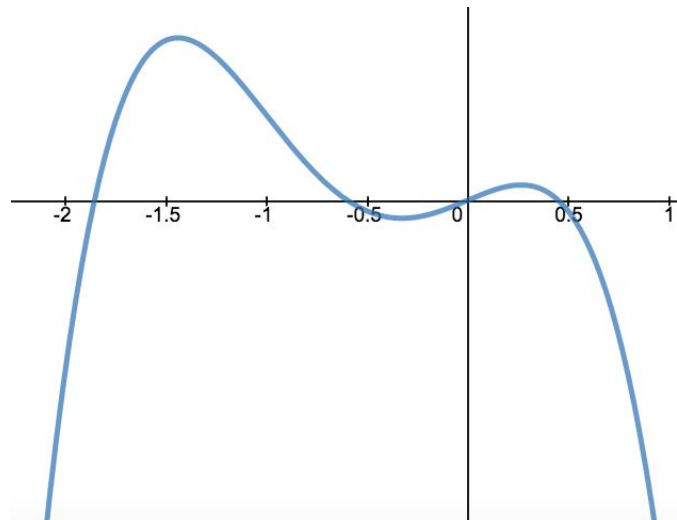
(Cirrito 20.1, p.646)

5. **(C5.4 - N) (CI)** The tangent line to a curve $y = g(x)$ at $x = 3$ has an x -intercept at $\frac{10}{3}$ and a y -intercept of -10 . What are the values of $g(3)$ and $g'(3)$?

(Cirrito 20.1, p.646)

6. **(C5.7 - N) (CI)** Here is a graph of a function. Sketch graphs of the **first** and **second** derivatives of this function.

(Cirrito 19.2, p.609)



7. **(C5.4 - N) (CI)** For $g(x) = \frac{1}{4}x^4 - \frac{4}{3}x^3 - \frac{5}{2}x^2 + 1$ determine:

(Cirrito 20.2, p.649)

- the equation of the derivative of $g(x)$.
- the zeroes of $g'(x)$.
- Hence or otherwise, find the coordinates of the stationary points of g .
- Hence or otherwise, find the intervals of increase and decrease of g .
- Sketch a graph of g . Then use your calculator and graph g and compare.

8. **(C5.4 - N) (CI)** For the function $f(x) = -x^4 - 2x^3 + 3x$ determine:

(Cirrito 20.2, p.649)

- the equation of the second derivative of $f(x)$.
- the zeroes of $f''(x)$.
- Hence or otherwise, find the x -coordinates of the inflection points of f .
- Hence or otherwise, find the intervals of concavity of f .
- I have included a graph of the **derivative of $f(x)$** . Use it to help you sketch a graph of f . Then use your calculator and graph f and then compare.

