

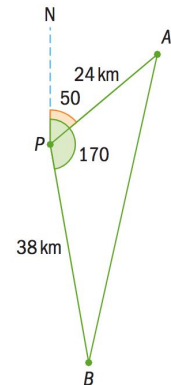
1. **(T1.9, R, CA)** Find the  $a^2b^4$  term in the expansion of  $(2a - 3b)^6$ . (Oxford 6.9, p.188)

2. **(T4.6, R, CA)** Given that  $P(E) = P(F) = 0.6$ , and  $P(E \cap F) = 0.24$   
(Oxford, 3.2, p.68)

- Write down  $P(E)$ .
- Explain why  $E$  and  $F$  are independent.
- Explain why  $E$  and  $F$  are not mutually exclusive
- Find  $P(E \cup F)$ .

3. **(T3.2, R, CA)** Two ships sail from the same port  $P$  at the same time. Ship A sails on a bearing of  $050^\circ$  for a distance of 24km before dropping anchor. Ship B sails on a bearing of  $170^\circ$  for a distance of 38 km before dropping anchor. Find the distance between the two ships when they are stationary.

(Cirrito 9.2, p.278)



4. **(T3.8, R, CI)** The owner of an ice cream shop tracks his annual sales and discovers that he sells a minimum of 5 gallons of ice cream on the first day of January, and a maximum of 37 gallons on the first day of July.

(Cirrito 10.4, p.351)

- Assuming the annual sales can be modeled by a cosine function, create an equation to model this situation. Let  $x$  represent the month.
- How many gallons would he expect to sell on the first day of April?
- During what month would he expect to sell 30 gallons of ice cream in one day?

5. **(T 4.4, R, CA)** Each day a clothing factory recorded the number of coats,  $x$ , it produces and the total production cost,  $y$ , in dollars. The results for nine days are shown in the following table.

(Oxford, 10.1, p. 332)

$x$	26	44	65	43	50	31	68	46	57
$y$	400	582	784	625	699	448	870	537	724

- Write down the equation of the regression line of  $y$  on  $x$ .

Use your regression line as a model to answer the following questions

- Interpret the meaning of the gradient and the  $y$ -intercept
- Estimate the cost of producing 70 coats
- The factory sells the boxes for \$19.99 each. Find the smallest number of coats that the factory should produce in one day in order to make a profit.

6. **(T1.3, R, CA)** A geometric series has nine terms, a common ratio of 2, and sum of 3577. Find the first term. *(Cirrito 8.2, p.252)*
7. **(T2.10, R, CA)** An equation of the form  $N(t) = \frac{a}{1+be^{-ct}}$ ,  $t \geq 0$ , where  $a, b$ , and  $c$  are positive constants represents a logistic curve. Logistic curves have been found useful when describing a population  $N$  that initially grows rapidly, but whose growth rate decreases after  $t$  reaches a certain value. A study of the growth of protozoa was found to display these characteristics. It was found that the population was well described if  $c = 1.12$ ,  $a = 100$ , and  $t$  measured time in days.  
*(Cirrito 7.2, p209)*
- If the initial population was 5 protozoa, find the value of  $b$ .
  - It was found that the growth rate was a maximum when the population size reached 50. How long did it take for this to occur?
  - Determine the optimum population size for the protozoa.
8. **(T. 25, 2.9, R, CI)** Solve the following:  
*(Cirrito 7.4, p219)*
- Each of the following equations for  $x$ , giving exact values in terms of the natural logarithm 'ln' or in terms of 'e'
    - $3^x = 6$
    - $\log_e(3x+1) - \log_e(4-x) = \log_e 4$
  - If  $f(x) = x + \frac{1}{x+1}$ ,  $x > 0$ , find  $f^{-1}(3)$ .
  - If  $f(x) = \sqrt{x-1}$  and  $g(x) = \frac{1}{x^2}$ , write down expressions for  $f(g(x))$  and  $g(f(x))$ .
    - For what values of  $x$  is  $f(g(x))$  defined?