

1. **(T3.5 - R) (CI)** The population (in thousands) of a species of butterfly in a nature sanctuary is modelled by the function:

$$P(t) = 3 + 2 \sin\left(\frac{3\pi t}{8}\right), \quad 0 \leq t \leq 12$$

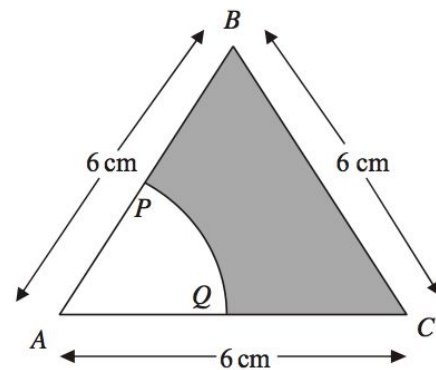
where  $t$  is the time in weeks after scientists first started making population estimates.

(Cirrito 10.5, p.361)

- What is the initial population?
- What are the largest and smallest populations?
- When does the population exceed 4,000 butterflies for the first time?

2. **(T3.1 - N) (CA)** The diagram shows an equilateral triangle ABC with sides of length 6 cm. (Cirrito 9.4, p287; Cirrito 9.7, p309)

P is the midpoint of AB.  
Q is the midpoint of AC.  
APQ is a sector of a circle, centre A.



- Calculate the length of the arc PQ of the sector
- Calculate the area of the shaded region.  
Give your answer correct to 3 significant figures.

3. **(T3.5 - E) (CI)** Draw the two special right triangles as well as graphs of  $y = \sin(x)$  and  $y = \cos(x)$ . Label the maximums, minimums and intercepts of these two graphs. (Cirrito 10.4, p.351)

- Solve  $\sqrt{2} \cos(x) + 1 = 0$  for  $-360^\circ \leq x \leq 360^\circ$
- Solve  $\sin^2(\theta) - 1 = 0$  for  $0 \leq \theta \leq 4\pi$

4. **(SP5.1, SP5.2, SP5.3 - R) (CA)** A survey is carried out to find the waiting times for 100 customers at a supermarket. The results are summarized in the table below: (Oxford 8.5, p171; Cirrito 13.5, p482)

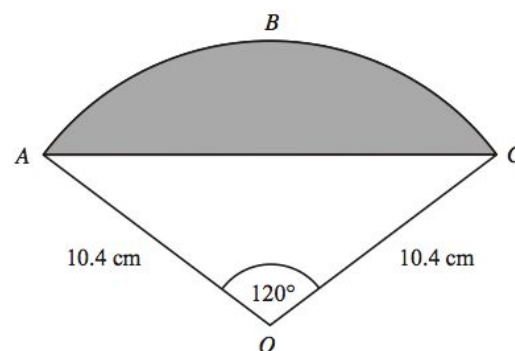
Waiting Time (sec)	0 - 20	20 - 40	40 - 60	60 - 80	80 - 100	100 - 120	120 - 140	140 - 160
Number of customers	5	15	33	21	11	7	5	2

- Calculate an estimate for the mean waiting time
- Estimate the value of the standard deviation as well as the variance of the waiting time.
- Draw a cumulative frequency graph (CFG) using graph paper
- Use the CFG to estimate the interquartile range.

5. **(A1.1 - E) (CI)** Three successive terms of a sequence are  $2k + 2$ ,  $5k + 1$  and  $10k + 2$ . Find the value(s) of  $k$  if: *(Cirrito, 8.2, p252)*

- the sequence is arithmetic;
- the sequence is geometric.

6. **(T3.1 - N) (CA)** The diagram shows a sector OABC of a circle with centre O. Given that  $OA = OC = 10.4$  cm and angle  $AOC = 120^\circ$ . *(Cirrito 9.4, p287; Cirrito 9.7, p309)*



- Calculate the length of the arc ABC of the sector. Give your answer correct to 3 significant figures.
- Calculate the area of the shaded segment ABC. Give your answer correct to 3 significant figures.

7. **(A1.1 - E) (CA)** Here are two more geometric series: *(Cirrito 8.2.4, p263)*

- $\frac{9}{2} + 3 + 2 + \frac{4}{3} + \dots$
- $240 - 60 + 15 - 3.75 + \dots$

- b. For each series,

- Find the common ratio,  $r$ .
- Use your calculator to find  $S_{10}$ ,  $S_{15}$  and  $S_{20}$ . Record the complete value (no rounding)

- c. Do you notice any patterns? Why do you think this is happening?

- d. Now use your calculator to evaluate  $S_{50}$ . Do you think your calculator is correct? Why or why not?

- e. For each series, predict the sum of an infinite number of terms.

8. **(A1.2 - N, F2.7 - E) (CI)** Solve  $\log_3(x - 2) + \log_3(x + 4) = 3$  for  $x$ . Use your TI-84 to graph and verify. Explain why there is only one solution for  $x$ . *(Cirrito 7.4, p221)*