1. [Maximum mark: 6]

The number of messages, M, that six randomly selected teenagers sent during the month of October is shown in the following table. The table also shows the time, T, that they spent talking on their phone during the same month.

Time spent talking on their phone (T minutes)	50	55	105	128	155	200
Number of messages (<i>M</i>)	358	340	740	731	800	<mark>992</mark>

The relationship between the variables can be modelled by the regression equation M = aT + b.

- (a) Write down the value of a and of b.
- (b) Use your regression equation to predict the number of messages sent by a teenager that spent 154 minutes talking on their phone in October.

2. [Maximum mark: 5]

Consider the lines L_1 and L_2 with respective equations

$$L_1: y = -\frac{2}{3}x + 9$$
 and $L_2: y = \frac{2}{5}x - \frac{19}{5}$.

(a) Find the point of intersection of L₁ and L₂.

A third line, L_3 , has gradient $-\frac{3}{4}$.

(b) Write down a direction vector for L_3 .

 L_3 passes through the intersection of L_1 and L_2 .

(c) Write down a vector equation for L_3 .

3. [Maximum mark: 7]

Let
$$f(x) = x - 8$$
, $g(x) = x^4 - 3$ and $h(x) = f(g(x))$.

(a) Find h(x).

Let C be a point on the graph of h. The tangent to the graph of h at C is parallel to the graph of f.

(b) Find the x-coordinate of C.

[5]

[2]

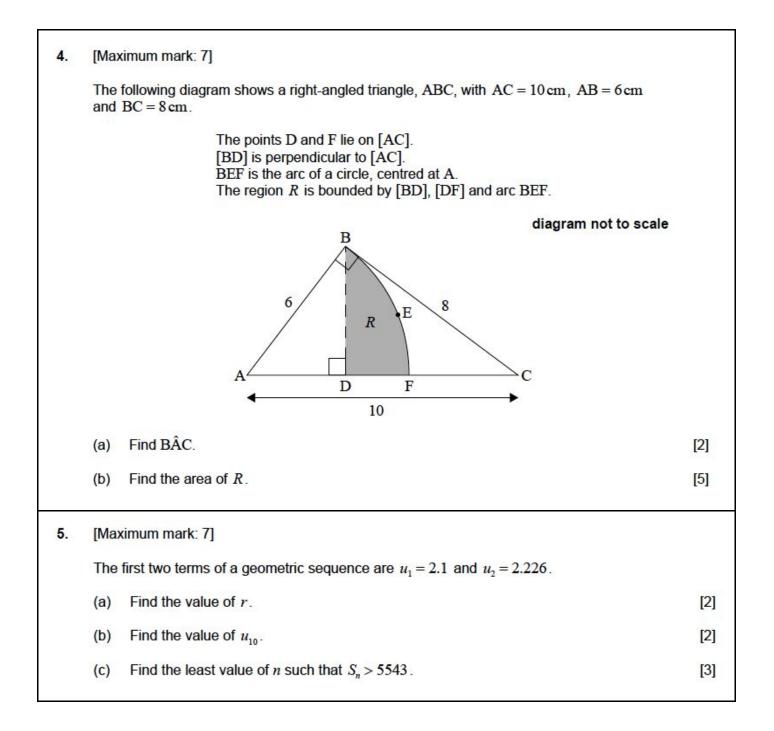
[3]

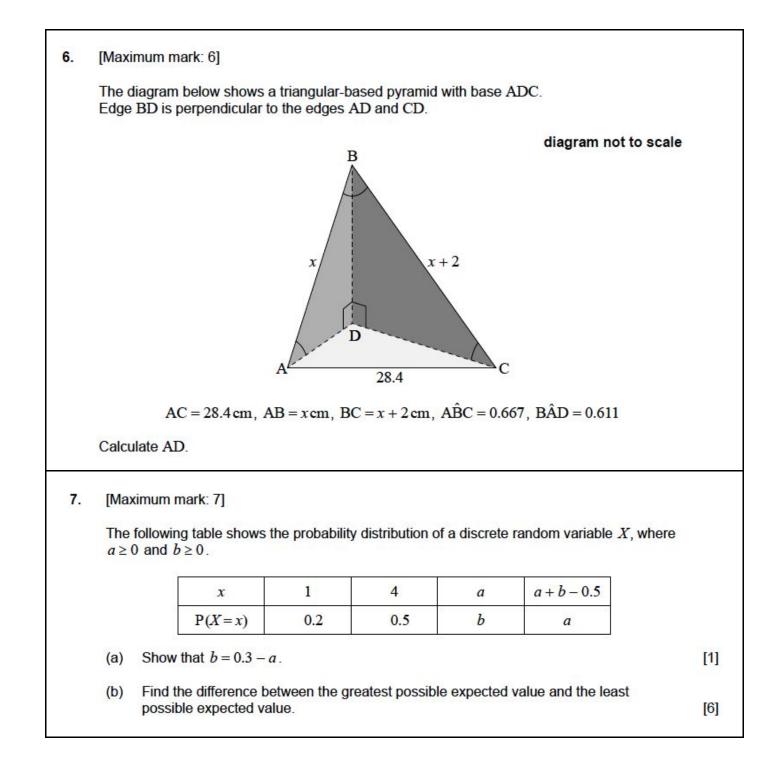
[3]

[2]

[1]

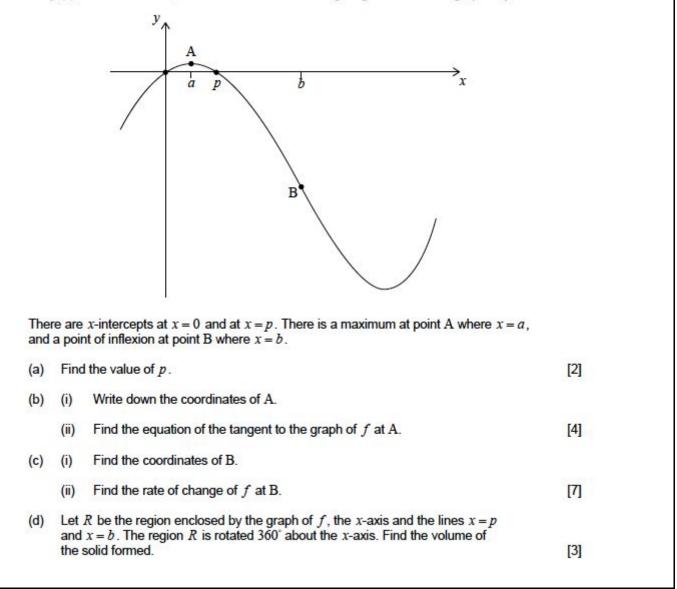
[2]





8. [Maximum mark: 16]

Let $f(x) = x^4 - 54x^2 + 60x$, for $-1 \le x \le 6$. The following diagram shows the graph of f.



9.	[Maximum mark: 15]							
	SpeedWay airline flies from city A to city B. The flight time is normally distributed with a mean of 260 minutes and a standard deviation of 15 minutes.							
	A flight is considered late if it takes longer than 275 minutes.							
	(a) Calculate the probability a flight is not late.							
	The flight is considered to be on time if it takes between m and 275 minutes. The probability that a flight is on time is 0.830.							
	(b) Find the value of m.							
	During a week, SpeedWay has 12 flights from city A to city B. The time taken for any flight is independent of the time taken by any other flight.							
	(c)	(i)	Calculate the probability that at least 7 of these flights are on time.					
		(ii)	Given that at least 7 of these flights are on time, find the probability that exactly 10 flights are on time.	[7]				
	SpeedWay increases the number of flights from city A to city B to 20 flights each week, and improves their efficiency so that more flights are on time. The probability that at least 19 flights are on time is 0.788.							
	(d)	A flig	ght is chosen at random. Calculate the probability that it is on time.	[3]				
10.	[Maxi	imum	mark: 14]					
	A rocket is travelling in a straight line, with an initial velocity of $140 \mathrm{ms}^{-1}$. It accelerates to a new velocity of $500 \mathrm{ms}^{-1}$ in two stages.							
	During the first stage its acceleration, ams^{-2} , after <i>t</i> seconds is given by $a(t) = 240 \sin(2t)$, where $0 \le t \le k$.							
	(a) Find an expression for the velocity, vms^{-1} , of the rocket during the first stage.							
	The f	irst sta	age continues for k seconds until the velocity of the rocket reaches $375 \mathrm{ms}^{-1}$.					
	(b)	Find t	the distance that the rocket travels during the first stage.	[4]				
	During the second stage, the rocket accelerates at a constant rate. The distance which the rocket travels during the second stage is the same as the distance it travels during the first stage.							
	(c)	Find t	the total time taken for the two stages.	[6]				