

B

5. For  $f(x) = x^2 - 6x + 5$ , find
- the missing coordinate in  $(x, ?)$
  - the slope of the tangent where  $x = 3$
  - the equation of the tangent in (b)
6. **Knowledge and Understanding:** For  $y = x^2 + 8x - 6$ , determine  $\frac{dy}{dx}$  from first principles.
7. Find the equation of the tangent for each given  $x$ -value.
- $y = x^2 + x - 3$ , where  $x = 4$
  - $y = 2x^2 - 7$ , where  $x = -2$
  - $f(x) = 3x^2 + 2x - 5$ , where  $x = -1$
  - $f(x) = 5x^2 - 8x + 3$ , where  $x = 1$
  - $y = x^2 + 8x + 12$ , where  $x = -4$
  - $f(x) = x^3 + 3x^2 - 2x + 4$ , where  $x = 1$
8. (a) Find the equation of the tangent to the curve of  $y = x^2 - 4x + 3$ , where  $x = 1$ .
- (b) Sketch the graph of the function and the tangent.
9. For  $f(x) = x^2 - 4x + 1$ , find
- the coordinates of point  $A$ , where  $x = 3$ , and of point  $B$ , where  $x = 5$
  - the equation of the secant  $AB$
  - the equation of the tangent at  $A$
  - the equation of the tangent at  $B$
10. For  $f(x) = 2x^2 - 3x - 5$ , find  $f(3)$  and  $f'(3)$ . Explain in words and with a diagram the meaning of the value and the derivative function.
11. **Communication:** If a function is not differentiable at  $x = a$ , what does this mean
- algebraically?
  - graphically?



12. A plane takes off from an airport. The table gives the plane's distance in kilometres from the airport at various times.

Time (h)	0	1	2	3	4	5	6
Distance (km)	0	300	800	1500	2300	2900	3300

- What is the average rate of change of distance with respect to time over the first four hours?
- Determine a possible algebraic model for the data.
- Use your model to estimate the speed of the plane at 3 h after take-off.

13. A tank holds 500 L of liquid, which is drained from the bottom of the tank. The volume,  $V$ , in litres, after  $t$  minutes is

$$V(t) = 500\left(1 - \frac{t}{90}\right)$$

- How much liquid remains in the tank after 45 minutes?
- What is the average rate of change of volume from 0 min to 60 min?
- How fast is the liquid draining at  $t = 45$  min?

14. **Application:** A population of raccoons in a park is modelled by the function  $P(t)$  at  $t$  months, the number of raccoons.

$$P(t) = 100 + 2t^2$$

Determine the rate at which the raccoon population is changing when the initial population has doubled in size.

15. The volume of a sphere is given by  $V = \frac{4}{3}\pi r^3$ , where  $V$  is the volume and  $r$  is the radius.
- Find the average rate of change of volume when the radius changes from 10 cm to 15 cm.
  - Find the rate of change of volume when the radius is 10 cm.

16. **Thinking, Inquiry, Problem Solving:** Find the equation of the line of intersection between the lines tangent to the curve  $y = x^2$  at  $x = 1$  and  $x = 2$ .

17. The average annual salary of a professional athlete is modelled by the function

$$S(x) = 246 + 64x$$

where  $S$  represents the average annual salary in millions of dollars and  $x$  is the number of years since 1982. Determine the rate at which the salary is changing in 2005.

18. A football is kicked up into the air. Its height,  $h$ , in metres, at  $t$  seconds can be modelled by  $h(t) = -5t^2 + 20t$ .
- Determine  $h'(2)$ .
  - What does  $h'(2)$  represent?

19. **Check Your Understanding:** Determine the equation of the tangent line to the curve  $y = 4x^3 - 3x + 6$  at point  $(1, 7)$ .

C

20. At what point on the graph of  $y = x^2 - 2x - y = 1$  is the tangent line horizontal?

21. Determine the coordinates of each point on the curve  $f(x) = 2x^3 - 7x^2 + 8x - 3$  where the tangent line is vertical.