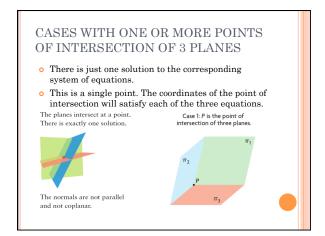
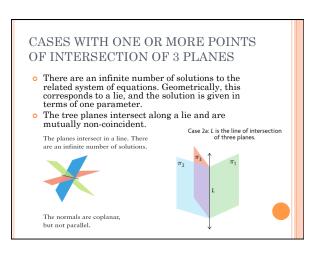
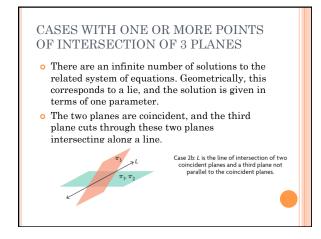
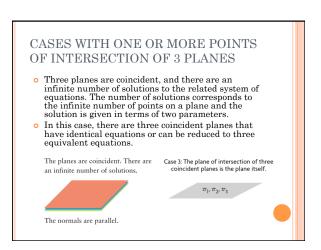


LEARNING GOALS • Recognize geometrically intersection three planes • Solve for the point and/or line of intersection of three planes









Using elementary operations to solve a system of three equations in three unknowns

Determine the intersection of the three planes with the equations x - y + z = -2, 2x - y - 2z = -9, and 3x + y - z = -2.

$$x - y + z = -2$$
, $2x - y - 2z = -9$, and $3x + y - z = -2$.

Selecting a strategy to determine the intersection of three planes

Determine the solution to the following system of equations:
①
$$2x - y + z = 1$$

$$2 3x - 5y + 4z = 3$$

$$3x + 2y - z = 0$$

More on solving a consistent system of equations

Determine the solution to the following system of equations:

②
$$4x - y - z = 5$$

$$38x - 2y - 2z = 10$$

CASES WITH NO POINTS OF INTERSECTIONS OF 3 PLANES

Three planes form a triangular prism as shown. This means that, if you consider any two of the three planes, they intersect in a line and each of these three lines is parallel to the others.

Case 1: A triangular prism is formed by three parallel lines.



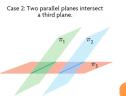


CASES WITH NO POINTS OF INTERSECTIONS OF 3 PLANES

Each of the parallel planes has a line of intersection with the third plane,

But there is no intersection between all three planes.

Two planes are parallel and distinct. The third plane is not parallel.



intersection.

and at least two are distinct.

CASES WITH NO POINTS OF INTERSECTIONS OF 3 PLANES

o All three planes do not have any points of



The normals are parallel.

CASES WITH NO POINTS OF INTERSECTIONS OF 3 PLANES

• All three planes do not have any points of intersection.

Case 4: Two planes are coincident; a third plane is parallel to and non-coincident with the first two planes. π_1,π_2

Selecting a strategy to solve an inconsistent system of equations

Determine the solution to the following system of equations:

①
$$x - y + z = 1$$

②
$$x + y + 2z = 2$$

$$3x - 5y - z = 1$$

Reasoning about an inconsistent system of equations

Determine the solution to the following system of equations:

①
$$x - y + 2z = -1$$

②
$$x - y + 2z = 3$$

$$3x - 3y + z = 0$$

Identifying coincident and parallel planes in an inconsistent system Solve the following system of equations:

①
$$x + y + z = 5$$

②
$$x + y + z = 4$$

$$3x + y + z = 5$$