



Fast Five

- 1. Isolate *y* from $x^2 + y^2 = 25$
- 2. Isolate *y* from 3x 2y + 10 = 0
- 3. Isolate *y* from $y^2 4x + 7 = 0$
- 4. Isolate *y* from $3x^2 2y^3 = 1$
- 5. Isolate y from $2x^5 + x^4y + y^5 = 36$
- > 6. Differentiate $36 = 2x^5 + x^4y + y^5$ on Wolframalpha

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- Up to this point, we have always defined functions by expressing one variable *explicitly* in terms of another i.e. y = f(x) = x² 1/x + x
 In other courses, we have also seen functions
- in other courses, we have also seen functions expressed *implicitly* i.e. in terms of both variables i.e. $x^2 + y^2 = 25$
- In simple implicit functions, we can always isolate the *y* term to rewrite the equation in *explicit* terms • i.e. $y = \pm \sqrt{(25 - x^2)}$
- > In other cases, rewriting an implicit relation is not so easy i.e. $2x^5+x^4y+y^5=36$

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"Level 7" Level Questions

- > 1. Find the equation of the lines that are tangent to the ellipse $x^2 + 4y^2 = 16$ AND also pass through the point (4,6)
- 2. Prove that the curves defined by x² y² = k and xy = p intersect orthogonally for all values of of the constants k and p. Illustrate with a sketch

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13

"Level 7" Level Questions • Find the equation of the tangent line at the point (a,b) on the curve x^{2/3} + y^{2/3} = 1. Hence, show that the distance between the x-and y-intercepts of the tangent line is independent of the point of tangency

Resources

- > You can watch the following ppt/pdfs:
- http://mrsantowski.tripod.com/2014MathHL/Resources/ Implicit_Diff_Part_1.pdf
- http://mrsantowski.tripod.com/2014MathHL/Resources/ Implicit_Diff_Part_2.pdf
- https://www.youtube.com/watch?v=ang_8ARu08g
- https://www.youtube.com/watch?v=rtZqpBSowJU
- https://www.youtube.com/watch?v=1scXr6g7HdA