### <u>Lesson 20 - Laws of</u> <u>Logarithms</u> B Math HL1 - Santowski

#### Lesson Objectives

11/1/2014

- Understand the rationale behind the "laws of logs"
- Apply the various laws of logarithms in solving equations and simplifying expressions

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Summary of Laws		
Logs as exponents	$b^{\log_b x} = x$	
Product Rule	$\log_a(mn) = \log_a m + \log_a n$	
Quotient Rule	$\log_{a}(m/n) = \log_{a}(m) - \log_{a}(n)$	
Power Rule	$Log_a(m^p) = (p) \times (log_a m)$	
11/1/2014	IB Math HI.1 - Santowski	3

# (A) Properties of Logarithms – Product Law Recall the laws for exponents → product of powers → (b<sup>x</sup>)(b<sup>y</sup>) = b<sup>(x+y)</sup> → so we ADD the exponents when we multiply powers For example → (2<sup>3</sup>)(2<sup>5</sup>) = 2<sup>(3+5)</sup> So we have our POWERS → 8 x 32 = 256

## (A) Properties of Logarithms – Product Law A. Now, let's consider this from the INVERSE viewpoint B. We have the ADDITION of the exponents 3 + 5 = 8 B. Ut recall from our work with logarithms, that the exponents are the OUTPUT of logarithmic functions S - 3 + 5 = 8 becomes log<sub>2</sub>8 + log<sub>2</sub>32 = log<sub>2</sub>256 A. Now, HOW do we get the right side of our equation to equal the left? B. Call that 8 x 32 = 256 So log<sub>2</sub>(8 x 32) = log<sub>2</sub>8 + log<sub>2</sub>32 = log<sub>2</sub>256















11











### (F) Examples

11/1/2014

Use the logarithm laws to simplify the following:

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19

- (a)  $\log_2 xy \log_2 x^2$
- (b)  $\log_2 \frac{8x^2}{y} + \log_2 2xy$
- (c)  $\log_3 9xy^2 \log_3 27xy$
- (d)  $\log_4(xy)^3 \log_4 xy$
- (e)  $\log_3 9x^4 \log_3 (3x)^2$

(F) Examples Exercise 2. Given  $\log_{10}(5.0) = 0.70 \ \log_{10}(2.0) = 0.30 \ \log_{10}(3.0) = 0.48, without a calculater, determine:$  $(1) <math>\log_{10}(6.0)$  (2)  $(1) \ \log_{10}(0.40)$ (3)  $\log_{10}(4)$  (3)  $(2) \ (3) \ \log_{10}(4.50)$ (4)  $\log_{10}(4.5)$  (9)  $\log_{10}(\sqrt{3.0})$ (5)  $\log_{10}(4.5)$  (10)  $\log_{10}(0.036)$