### Study Aid

- See Lesson 1.4,
   Examples 1 to 4.
- Try Chapter Review Questions 7 to 9.

## FREQUENTLY ASKED Questions

## Q: How can you use algebra to solve a linear system?

A1: You can use a substitution strategy. Express one variable in one of the equations in terms of the other variable. Substitute this expression into the other equation, and solve for the remaining variable. Finally, substitute the solved value into the expression to determine the value of the other variable.

#### **EXAMPLE**

Solve the system.

$$2x + y = 29$$

(2)

$$4x - 3y = 18$$

From (1), y = 29 - 2x.

Substitute this expression for y into ② and solve for x.

$$4x - 3(29 - 2x) = 18$$

$$4x - 87 + 6x = 18$$

$$10x - 87 = 18$$

$$10x = 18 + 87$$

$$10x = 105$$

$$x = 10.5$$

Determine y by substituting this value of x into the expression for y.

$$y = 29 - 2(10.5)$$

$$y = 8$$

The solution is x = 10.5 and y = 8.

**A2:** You can use an elimination strategy. Eliminate *x* or *y* from the system by multiplying one or both equations by a constant other than zero, and then adding or subtracting the equations. Solve the resulting equation for the remaining variable. Substitute the solved value into one of the original equations, and determine the value of the other variable.

#### **EXAMPLE**

Solve the system.

$$2x + y = 29$$

$$4x - 3y = 18$$

Study | Aid

See Lesson 1.6,

Examples 1 and 3.

Try Chapter Review

Questions 12 to 16.

#### Solution

#### Eliminating x

Multiply (1) by 2 and subtract.

 $(1) \times 2$ 

$$4x + 2y = 58$$

$$\frac{4x - 3y = 18}{5y = 40}$$

$$y = 8$$

Substitute y = 8 into ①.

$$2x + 8 = 29$$

$$2x = 29 - 8$$

$$2x = 21$$

$$x = 10.5$$

#### Eliminating y

Multiply (1) by 3 and add.

$$6x + 3y = 87$$
 (1) × 3

$$\frac{4x - 3y = 18}{10x = 105}$$

$$x = 10.5$$

Substitute 
$$x = 10.5$$
 into ①.

$$2(10.5) + y = 29$$

$$21 + y = 29$$

$$y = 29 - 21$$

$$y = 8$$

The solution is x = 10.5 and y = 8.

# Q: When you use elimination, how do you decide whether to add or subtract the equations?

A: If the coefficients of the variable you want to eliminate are the same, subtract. If the coefficients are opposites, add.

# Q: How do you decide whether to use graphs, substitution, or elimination to solve a linear system?

A: The strategy you use will depend on what degree of accuracy is required, what form the equations are written in, and whether more than just the solution is required. Algebraic solutions give exact answers, whereas hand-drawn graphs often do not.

## Use graphs if

- you do not need an exact answer
- you need to look for trends or compare the graphs before and after the point of intersection
- you have a graphing calculator and both equations are in the form y = mx + b

#### Use substitution if

- · you need exact answers
- one of the variables in the equation is already isolated, ready to make the substitution (that is, in the form y = mx + b)
- you can easily rearrange one equation to isolate a variable

#### Use elimination if

- you need exact answers
- both equations are in the form Ax + By = C or Ax + By + C = 0

## Study | Aid

- See Lesson 1.6, Examples 1 to 3.
- Try Chapter Review Questions 12 and 15.

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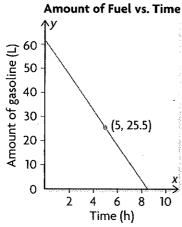
## **PRACTICE** Questions

#### Lesson 1.1

- 1. Sheila is planning to visit relatives in England and Spain. On the day that she wants to buy the currencies for her trip, one euro costs \$1.50 and one British pound costs \$2.00. What combinations of these currencies can Sheila buy for \$700? Use three different strategies to show the possible combinations.
- 2. After a fundraiser, the treasurer for a minor soccer league invested some of the money in a savings account that paid 2.5%/year and the rest in a government bond that paid 3.5%/year. After one year, the money earned \$140 in interest. Define two variables, write an equation, and draw a graph for this information.

#### Lesson 1.2

3. Gary drove his pickup truck from Cornwall to Chatham. He left Cornwall at 8:15 a.m. and drove at a steady 100 km/h along Highway 401. The graph below shows how the fuel in the tank varied over time.



- a) What do the coordinates of the point (5, 25.5) tell you about the amount of fuel?
- **b)** How much fuel was in the tank at 11:45 a.m.?
- The low fuel warning light came on when 6 L of fuel remained. At what time did this light come on?

4. Readycars charges \$59/day plus \$0.14/km to rent a car. Bestcars charges \$69/day plus \$0.11/km. Describe three different strategies you could use to compare these two rental rates. What advice would you give someone who wants to rent a car from one of these companies?

#### Lesson 1.3

**5.** Solve each linear system graphically.

a) 
$$x + y = 2$$
  
 $x = 2y + 2$ 

**b)** 
$$y - x = 1$$
  $2x - y = 1$ 

- 6. Tools-R-Us rents snowblowers for a base fee of \$20 plus \$8/h. Randy's Rentals rents snowblowers for a base fee of \$12 plus \$10/h.
  - a) Create an equation that represents the cost of renting a snowblower from Tools-R-Us.
  - **b)** Create the corresponding equation for Randy's Rentals.
  - Solve the system of equations graphically.
  - **d)** What does the point of intersection mean in this situation?



#### Lesson 1.4

**7.** Use substitution to solve each system.

a) 
$$2x + 3y = 7$$
  
 $-2x - 1 = y$ 

c) 
$$5x + 2y = 18$$
  
 $2x + 3y = 16$ 

**b)** 
$$3x - 4y = 5$$

**b)** 
$$3x - 4y = 5$$
  $x - y = 5$  **d)**  $9 = 6x - 3y$   $4x - 3y = 5$ 

**8.** Courtney paid a one-time registration fee to join a fitness club. She also pays a monthly fee. After three months, she had paid \$315. After seven months, she had paid \$535. Determine the registration fee and the monthly fee.

- 9. A rectangle has a perimeter of 40 m. Its length is 2 m greater than its width.
  - a) Represent this situation with a linear system.
  - **b)** Solve the linear system using substitution.
  - c) What do the numbers in the solution represent? Explain.

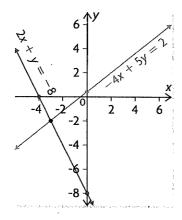
#### Lesson 1.5

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10. a) Which linear system below is equivalent to the system that is shown in the graph?



**A.** 
$$2x - 5y = 4$$
 **B.**  $-x + y = 1$ 

**A.** 
$$2x - 5y = 4$$
 **B.**  $x - 3y = -1$   $-x + y = 1$   $2x + y = 4$ 

- **b)** Use addition and subtraction to create another linear system that is equivalent to the system in the graph.
- Use multiplication to create another linear system that is equivalent to the system in the graph.
- 11. a) Create two linear systems that are equivalent to the following system. -2x - 3y = 53x - y = 9
  - **b)** Verify that all three systems have the same solution.

#### Lesson 1.6

**12.** Use elimination to solve each linear system.

a) 
$$2x - 3y = 13$$
  
 $5x - y = 13$ 

$$2x - 3y = 13$$
 c)  $3x + 21 = 5y$   
 $5x - y = 13$   $4y + 6 = -9x$ 

**b)** 
$$x - 3y = 0$$
  
 $3x - 2y = -7$ 

**b)** 
$$x - 3y = 0$$
  
 $3x - 2y = -7$   
**d)**  $x - \frac{1}{3}y = 1$   
 $\frac{2}{3}x - \frac{1}{4}y = -1$ 

- 13. Lyle needs 200 g of chocolate that is 86% cocoa for a cake recipe. He has one kind of chocolate that is 99% cocoa and another kind that is 70% cocoa. How much of each kind of chocolate does he need to make the cake? Round your answer to the nearest gram.
- 14. A Grade 10 class is raising money for a schoolbuilding project in Uganda. To buy 35 desks and 3 chalkboards, the students need to raise \$2082. To buy 40 desks and 2 chalkboards, they need to raise \$2238. Determine the cost of a desk and the cost of a chalkboard.



**15.** Solve the linear system. 2(2x-1)-(y-4)=11

$$2(2x - 1) - (y - 4) = 11$$
  
3(1 - x) - 2(y - 3) = -7

- **16.** Juan is a cashier at a variety store. He has a total of \$580 in bills. He has 76 bills, consisting of \$5 bills and \$10 bills. How many of each type does he have?
- 17. a) Sketch a linear system that has no solution.
  - **b)** Determine two possible equations that could represent both lines in your sketch.
  - c) Explain how the slopes of these lines are related.
- **18.** The linear system 6x + 5y = 10 and ax + 2y = b has an infinite number of solutions. Determine a and b.

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Number of 500 g Cartons	Number of 750 g Bags
50	1150
100	1117
150	1083
200	1050 -
1000	517
1500	183
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Process	Checklist

- Questions 1 and 2: Did you connect and compare the representations?
- Questions 5 and 9: Did you communicate your thinking clearly?
- Questions 7 and 8: Did you problem solve by selecting and applying appropriate strategies?

- 1. The Rainin' Raisins company packs raisins in 500 g cartons and 750 g bags. One day, 887.5 kg of raisins were packed into full cartons and bags. Ben wondered how many cartons and how many bags could have been packed. He began to chart some possible combinations shown at the left. Use a graph and an equation to show all the possible combinations.
- 2. Milk is leaking from a carton at a rate of 4 mL/min. There is 1500 mL of milk in the carton at 8:30 a.m.
  - a) Write an equation and draw a graph for this situation.
  - b) Determine graphically when 1 L of milk will be left in the carton.
  - c) Use your equation to determine algebraically when 1 L of milk will be left in the carton.
- 3. Solve each system of equations. Use a different strategy for each system.

a) 
$$3x + y = -2$$
  
 $5x - y = -10$ 

**b)** 
$$2x + 7 = y$$

c) 
$$3x + 5y = -9$$
  
 $2x - y = 7$ 

- 5x y = -10 -3x 2y = 10 2x y = 7**4.** Shannon needs 20 g of 80% gold to make a pendant. She has some
- 85% gold and some 70% gold, from broken jewellery, and wants to know how much of each she should use. Determine the quantity of each alloy that she should use.
- 5. How would you explain to someone why it makes sense that you can add two equations and subtract them to create an equivalent system of linear equations?
- **6. a)** Create two linear systems that are equivalent to the system 3x + 4y = -8 and x 2y = 9.
  - b) Verify that all three systems are equivalent.
- 7. In his spare time, Kim likes to go cycling. He cycles partly on paved surfaces and partly off-road, through hilly and wooded areas. He cycles at 25 km/h on paved surfaces and at 10 km/h off-road. One day, he cycled 41 km in 2 h. How far did he cycle off-road?
- **8.** Last summer, Betty earned \$4200 by painting houses. She invested some of the money in a savings account that paid 3.5%/year and the rest in a government bond that paid 4.5%/year. After one year, she has earned \$174 in interest. How much did she invest at each rate?
- 9. Explain how you know that this system of equations has no solution.

$$15 - 6y = 9x$$

$$3x + 2y = 8$$