

A. Lesson Objectives

- a. Review the key ideas from our Composition & Transformations lesson
- b. Highlight the key features being communicated in the vertex form of a quadratic function
- c. Graphically and algebraically analyze quadratic equations written in vertex form
- d. Apply the vertex form of quadratic functions to mathematical models

B. REVIEW of Exploration in L24: Transformations

- a. Compare the PARENT function $f(x) = x^2$ with the following functions: (GRAPH ON TI84)

| $y = x^2$ | $y = 2x^2$ | $y = 3x^2$ | $y = 4x^2$ |
|-----------|------------|------------|------------|
| | | | |

- b. Compare the PARENT function $f(x) = x^2$ with the following functions:

| $y = x^2$ | $y = \frac{1}{2} x^2$ | $y = \frac{1}{3} x^2$ | $y = \frac{1}{4} x^2$ |
|-----------|-----------------------|-----------------------|-----------------------|
| | | | |

- c. Compare the PARENT function $f(x) = x^2$ with the following functions:

| $y = x^2$ | $y = -x^2$ |
|-----------|------------|
| | |

The Vertex Form of A Quadratic Function

Lesson 25

d. Compare the PARENT function $f(x) = x^2$ with the following functions:

| $y = x^2$ | $y = (x - 1)^2$ | $y = (x - 2)^2$ | $y = (x - 3)^2$ |
|-----------|-----------------|-----------------|-----------------|
| | | | |

e. Compare the PARENT function $f(x) = x^2$ with the following functions:

| $y = x^2$ | $y = (x + 1)^2$ | $y = (x + 2)^2$ | $y = (x + 3)^2$ |
|-----------|-----------------|-----------------|-----------------|
| | | | |

f. Compare the PARENT function $f(x) = x^2$ with the following functions:

| $y = x^2$ | $y = x^2 + 1$ | $y = x^2 + 2$ | $y = x^2 + 3$ |
|-----------|---------------|---------------|---------------|
| | | | |

g. Compare the PARENT function $f(x) = x^2$ with the following functions:

| $y = x^2$ | $y = x^2 - 1$ | $y = x^2 - 2$ | $y = x^2 - 3$ |
|-----------|---------------|---------------|---------------|
| | | | |

The Vertex Form of A Quadratic Function

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C. Transformations: Extend Your Thinking

Compare the PARENT function $f(x) = x^2$ with the following functions (NO GRAPHING ON TI84)

| | | | |
|---------------------|----------------------|---------------------------------|----------------------|
| $y = (x - 5)^2 + 2$ | $y = -(x + 2)^2 + 4$ | $y = -\frac{1}{2}(x - 1)^2 - 3$ | $y = a(x - h)^2 + k$ |
| | | | |

D. Analysis of Quadratic Functions in Vertex Form: Graphic & Algebraic

WITHOUT THE USE OF THE GRAPHING CALCULATOR, analyze the quadratic function $y = \frac{1}{2}(x - 4)^2 - 2$

| | |
|--|--|
| <p>(1) direction of opening:</p> <p>(2) vertex?</p> <p>(3) max/min value?</p> <p>(4) y-intercept?</p> <p>(5) a non-intercept point?</p> <p>(6) zeroes?</p> | |
|--|--|

The Vertex Form of A Quadratic Function | Lesson 25

WITHOUT THE USE OF THE GRAPHING CALCULATOR, analyze the quadratic function $y = -2(x + 1)^2 + 10$

(1) direction of opening:

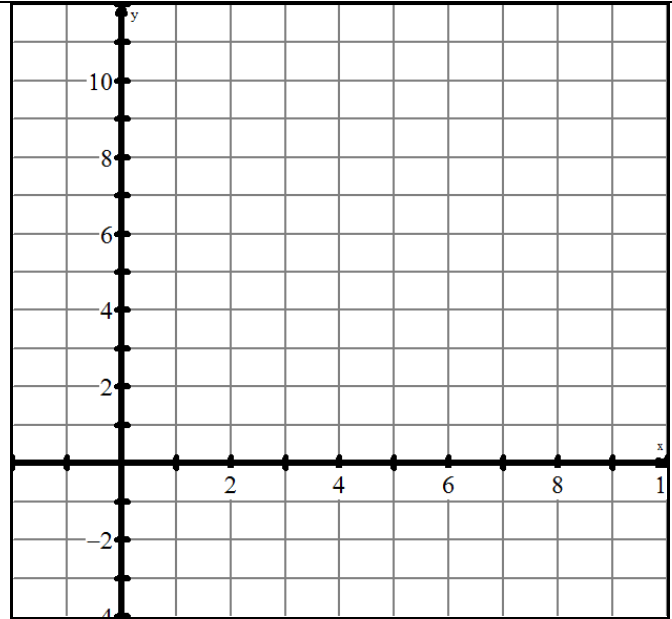
(2) vertex?

(3) max/min value?

(4) y-intercept?

(5) a non-intercept point?

(6) zeroes?



E. Applications of Quadratic Functions: Using Vertex Form

a. Example 1: A ball is hit into the air. Its height H (in meters above the ground) after t seconds is modelled by the function $H(t) = -5(t - 4)^2 + 120$. Answer the following questions WITHOUT THE USE OF THE TI84

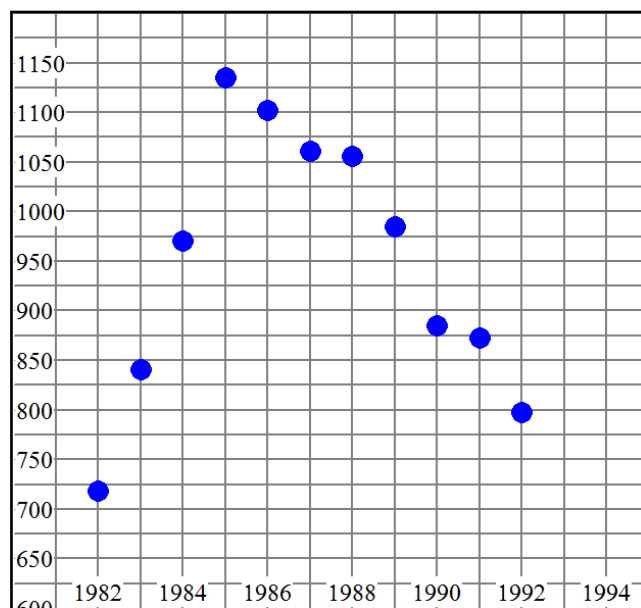
- i. In which direction does the parabola open/ how do you know?
- ii. Determine the initial height of the ball. Show the analysis that leads to your answer.
- iii. What are the co-ordinates of the vertex? What does the vertex represent in this situation?
- iv. Determine one other co-ordinate on the curve and interpret its meaning.
- v. When does the ball hit the ground? Show the analysis that leads to your answer.
- vi. State the domain and range for this model. Explain the reasoning for your answers.
- vii. Sketch the flight path of the ball
- viii. CONFIRM your answers using the TI84

E. Applications of Quadratic Functions: Using Vertex Form

- b. Example 2: The following table shows how many new cars were sold (in thousands) in Canada from 1982 until 1992:

| Year | 1982 | 1983 | 1984 | 1985 | 1986 | 1987 | 1988 | 1989 | 1990 | 1991 | 1992 |
|-----------|------|------|------|------|------|------|------|------|------|------|------|
| Cars sold | 718 | 841 | 971 | 1135 | 1102 | 1061 | 1056 | 985 | 885 | 873 | 798 |

- i. Draw the curve of best fit
 - ii. Estimate the coordinates of the vertex.
 - iii. Determine an algebraic function that models this data
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- iv. Use the algebraic model to predict how many new cars were sold in 1994?



- v. How would you describe the trend in car sales between the years 1982 – 1986?
- vi. How would you describe the trend in car sales between the years 1986 – 1992? Give two reasons why.
- vii. How well does the model work to predict the car sales in 2000 and beyond? Why?
- viii. Check the accuracy of your model using your TI-84 and an appropriate regression.