

## IM2 Problem Set 4.8 - Linear Relations

BIG PICTURE of this UNIT:	<ul style="list-style-type: none"><li>• What is meant by the term FUNCTIONS and how do we work with them?</li><li>• mastery with working with basics &amp; applications of linear functions</li><li>• mastery with working with basics &amp; applications of linear systems</li><li>• understanding basics of function concepts and apply them to lines &amp; linear systems</li></ul>
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### Part 1 - Skills/Concepts Review

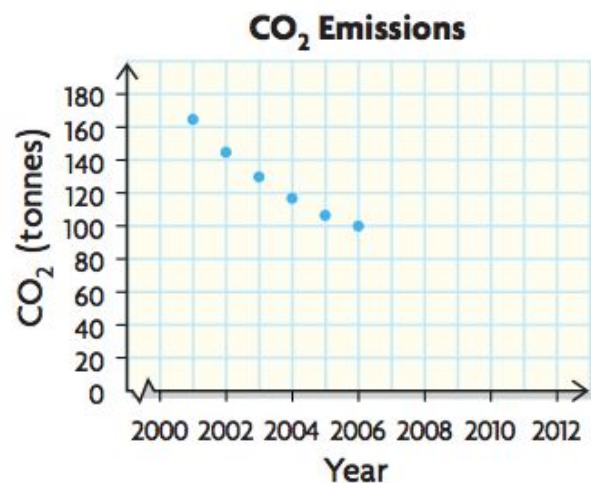
- (CI)** Graph the following linear functions, given the conditions indicated:
  - $g(x) = \frac{3}{4}x + 2$  on the domain of  $[-4, 8)$
  - $2x - 5y - 20 = 0$  on the range of  $\{-6 < y \leq 6\}$
  - $y - 5 = -\frac{1}{2}(x + 4)$  on the range of  $(-10, 10]$
- (CI)** For the following functions, evaluate the function as required:
  - If  $h(x) = 3x - 5$ , evaluate  $h(-2)$ ,  $h(6)$ ,  $h(a)$ ,  $h(2x + 1)$
  - If  $E(x) = 5 \times 2^x$ , evaluate  $E(3)$ ,  $E(0)$ ,  $E(-2)$ ,  $E(a)$ ,  $E(1 - 3x)$
  - If  $P(x) = (x + 3)(x - 1)$ , evaluate  $P(-1)$ ,  $P(4)$ ,  $P(-3)$ ,  $P(k)$
- (CA)** Decide whether each ordered pair is a solution to the given system of equations:
  - $(2, -1)$ ;  $3x + 2y = 4$  and  $-x + 3y = -5$
  - $(1, 4)$ ;  $x + y = 5$  and  $2x + 2y = 8$
- (CA)** Use DESMOS to work through the following question:
  - Graph the linear function defined by  $3x + 2y = -3$
  - Multiply this equation by 2 and describe what happens when you graph the new function.
  - Multiply this equation by -5 and describe what happens when you graph the new function.
  - Graph the linear function defined by  $-2x + 5y = 21$
  - Multiply this equation by 3 and describe what happens when you graph the new function.
  - Multiply this equation by -2 and describe what happens when you graph the new function.
- (CI)** Use the elimination method to solve the linear systems defined by the following pairs of equations. Verify your solutions using (i) algebra and (ii) your graphing calculator.
  - $L_1: 3x + 2y = -3$  and  $L_2: -2x + 5y = 21$ .
  - $L_1: x - 4y = -1$  and  $L_2: -3x + 8y = -2$ .
- (CI)** Use the substitution method to solve the linear systems defined by the following pairs of equations. Verify your solutions using (i) algebra and (ii) your graphing calculator.
  - $L_1: y = 4x - 7$  and  $L_2: 2x - 3y = 6$
  - $L_1: f(x) = 5x - 8$  and  $L_2: 10x - 5y = 7$

## Part 2 - Skills/Concepts Application Problems

7. **(CA)** Joanna is considering three job offers. Pheonix Phasions offers her \$1500/month plus 2.5% commission; Styles By Styx offers her \$1250/month plus 5.5% commission; Chanel No 2 offers here \$36,000 per year, regardless of her sales.
- Write equations for the salary offer from each company.
  - Graph each equation on your calculator.
  - How many intersection points are there and what does each intersection point mean?
  - Which job offer should she accept? Explain your choice.
8. **(CA)** Six cups of coffee and a dozen muffins originally cost \$15.35. The price of coffee increases by 10% and the price of the muffins increases by 12%. So the new cost for six coffee and a dozen muffins is \$17.06. Determine the new price of one cup of coffee and the new price of one muffin.
9. **(CI)** A linear systems is defined by the equations  $ax + 2y = -5$  and  $3x - 4y = 1$  may/may not intersect - it depends upon the value of  $a$ .
- Find value(s) of  $a$  such that two lines DO NOT intersect.
  - Hence, find value(s) of  $a$  such that the lines DO intersect.
  - EXTENSION:** What is/are the intersection point(s) - Express your answer in terms of  $a$ ?
10. **(CA)** The function  $f$  is defined by  $f(x) = 2x + 3$  and the function  $g$  is defined as  $g(x) = 3x + 5$ . Answer the following questions about these functions.
- Evaluate:    i.  $f(3) - f(2)$     ii.  $f(4) - f(3)$     iii.  $f(5) - f(4)$     iv.  $f(a + 1) - f(a)$
  - What observation do you make and why does this happen?
  - Evaluate:    i.  $g(3) - g(2)$     ii.  $g(4) - g(3)$     iii.  $g(5) - g(4)$     iv.  $g(a + 1) - g(a)$
  - What observation do you make and why does this happen?
  - Evaluate    i.  $g(f(-5))$     ii.  $f(g(2))$     iii.  $f(g(x))$     iv.  $g(f(x))$ .

11. **(CA)** To help protect the environment, a steel factory is thinking about setting new standards for its carbon dioxide CO<sub>2</sub> emissions. By 2022, the factory wants to emit less than 70 tonnes of CO<sub>2</sub> per year. The data table and a scatter-plot are presented below.

CO <sub>2</sub> (tonnes)	165	145	130	117	107	100
Year	2001	2002	2003	2004	2005	2006



- Graph the data set on your TI-84.
- Determine an equation for the line of best fit. Predict the amount of CO<sub>2</sub> emissions in 2012.
- Explain why Mr R thinks that a curve would fit the data better.
- Draw a curve of best fit and predict the amount of CO<sub>2</sub> emissions in 2012.
- Which prediction do you think is better? Explain your reasoning.

### Part 3 - Extension Problems

12. A function is defined by the following **recursion** formula:  $f(n) = f(n - 1) - f(n - 2) + n$ ;  $f(1) = 1$  and  $f(2) = 1$  as well.
- Evaluate  $f(3)$ ,  $f(4)$ ,  $f(5)$  and  $f(6)$
  - Hence or otherwise, evaluate  $f(2018)$
13. A three-dimensional rectangular box with dimensions X, Y and Z has faces whose surface areas are 24, 24, 48, 48, 72 and 72. What is  $X + Y + Z$  equal to?

### HOMEWORK PROBLEMS:

- Nelson 10, Chap 1.4, p39, Q9bdf and Q6 and Q7
- Nelson 10, Chap 1.6, p55, Q6de, 12