BIG PICTURE of this Unit

- How can we extend our geometry skills with triangles to go beyond right triangles to (i) obtuse triangles and (ii) circles and Cartesian Planes?
- What do triangles have to do with sinusoidal functions in the first place?
- How can we connect previously learned function concepts and skills to sinusoidal functions?
- How can use the equation of a sinusoidal function be used to analyze for key features of a graph of a sinusoidal curve?
- When and how can triangles and sinusoidal functions be used to model real world scenarios?
- 1. (CI Ideally) The average monthly temperature in a region of Australia is modelled by the function

 $T(t) = 9 + 23\cos(30t)$, where T is the temperature in degrees Celsius and t is the month of the year. For t = 0, the

month is January. {6,15,17,20}

- a. Explain how to use the axis of the curve and the amplitude to determine the maximum and minimum values of the function.
- b. Determine the period of the function from the graph. Verify your answer algebraically.
- c. Prepare a table for $0 \le t \le 13$. (Ideally, no calculator, but you may use one if needed \Rightarrow HINT: 30-60-90 right triangle??)
- d. Prepare a scatter plot of the data (WITHOUT the TI-84).
- e. Verify the graph in Q(d) by using a graphing calculator.
- f. Explain how to sketch a similar graph using transformations of y = cos(t).
- 2. (CA) Solve the following word problems. {8,9,10}

A triangular lot sits at the corner of two streets that intersect	11. From the top of an 8 m house, the angle of
at an angle of 58°. One street side of the lot is 32 meters	elevation to the top of a flagpole across the street
long and the other street side is 40 meters long.	is 9°. The angle of depression is 22° to the base of the flagpole. How tall is the flagpole?
(a) This triangular field is to be fenced. Determine the total	9°
perimeter of the field.	
(b) Determine the total area of the field.	8 m

- 3. (CA) Graph the point A(-6,-12). The terminal arm of an angle goes through this point. {1,11,12}
 - a. Draw the angle described in this question. Label the principle angle and the related acute angle.
 - b. Determine the sine and cosine and tangent ratios for this angle. (Use EXACT values for the hypotenuse)
 - c. Explain WHY the sine and cosine ratios are negative.
 - d. Determine the measure of the principle angle and the related acute angles.
 - e. Determine the value of the following: (i) $\sin^{-1}\left(-\frac{12}{\sqrt{180}}\right)$, (ii) $\cos^{-1}\left(-\frac{6}{\sqrt{180}}\right)$, (iii) $\tan^{-1}\left(-2\right)$
 - f. Explain WHY your answers for Qd and Qe are NOT the same? Should they be?
 - g. Sketch two cycles of y = sin(x) as well as y = cos(x) and use this graph to explain the reason(s) behind what is happening in Qd, Qe, Qf
- 4. (CI) Graph the following data sets and then determine the equation of the sinusoidal function that best matches the data set. {17,19,20}



Problem Set 6.10

- 5. (CA) The maximum height of a Ferris wheel is 35 m. The wheel takes 2 min to make one revolution. Passengers board the Ferris wheel 2 m above the ground at the bottom of its rotation. {17,19}
 - a. Write an equation to represent the position of a passenger at any time, t, in seconds.
 - b. How high is the passenger after 45 s?
 - c. The ride lasts for 4 min. At what time(s) will the passenger be at the maximum height during this ride?
- 6. (CI Ideally) The figure below shows a long rectangular strip of paper, one corner of which has been folded over to meet the opposite edge, thterby creating a 30 degree angle. Given that the width of the strip of paper is 12 inches, find the length of the crease. {3,4,5}





Higher Level Questions for More Complex Concepts OR an EXTENSION of basic concepts involved with triangle trigonometry and sinusoidal functions.

See worksheet below

Problem Set 6.10

Worksheet on Radians

When a central angle intercepts an arc that has the same length as a radius of the circle, the measure of this angle is defined to be one **radian**.



The circumference of a circle is 2π r, where r is the length of a radius. There are 2π radians in one complete revolution about a point and one complete revolution equals 360° .

 2π radians = 360° π radians = 180° 1 radian $\approx 57.3^{\circ}$

Convert each degree measure to radian measure.

Convert each radian measure to degree measure.

1. 120° 2. -245° 3. $\frac{\pi}{3}$ radians 4. $-\frac{3\pi}{4}$ radians



In which quadrant or on which axis does the terminal side of the angle lie?

5.
$$\frac{4\pi}{3}$$
 6. $-\frac{5\pi}{4}$ 7. $\frac{9\pi}{2}$

Problem Set 6.10

In which quadrant, or on which axis, does the terminal side of the each angle lie?					
8. 150°	9. 210°	1060°	11. 180°		
12240°	13. 540°	14. 2 <i>π</i>	15. $\frac{\pi}{3}$		
16. $\frac{3\pi}{4}$	17. $\frac{7\pi}{3}$	18. $\frac{5\pi}{4}$	19. $\frac{10\pi}{3}$		
Convert each degree measure to radian measure.					
20. 150°	21. 210°	22. 45°	23. 240°		
Each radian measure to degree measure.					

~ .	π	π	5π	-7π
24.	_	25. —	26. —	27. —
	6	4	6	6

In exercises 28 to 31, find the measure of the central angle in both degrees and radians with the given radius and arc length.

28) r = 4 cm, s = 16 cm 29) r = 5 m, s = 4 m 30) r = 3.2 in, s = 7.8 in

31) The minute hand on the clock at the City Hall clock in Stratford measures 2.2 metres from the tip to the axle.

a) Through what angle does the minute hand pass between 7:07 A.M. and 7:43 A.M.?

b) What distance does the tip of the minute hand travel during this period?

32) You are at the stern of a paddle boat and observe that the paddle wheel has a radius of 10ft and makes 15 revolutions per minute. What is the speed of the paddle boat with respect to the water?

33) A car with a 12 inch radius wheel is moving with a velocity of 65 mph. Find the angular velocity of the tire in revolutions per second.