

BIG PICTURE of this UNIT:

- How do we WORK WITH & EXTEND the concept of “functions”
- Why are quadratic equations written in different forms?
- How do we EXTEND and APPLY our knowledge of quadratic functions, beyond the basics of IM2?

This lesson will be based upon a STUDENT DIRECTED DISCUSSION model in your groups, you should be having DISCUSSIONS about how to think and work through and then present the solutions to the following questions. So, discuss & prepare solutions to the following questions. Record the key ideas of your discussions/solutions in your notebook. Then, once you have had your discussions, present your solutions on the board. Solutions do NOT necessarily NEED to be correct – they simply form the basis for DISCUSSIONS!!!! If your group has (i) multiple solutions that lead to the same answers OR (ii) same/different solutions that lead to different answers, present them ANYWAY!!

- Write the equations of the following parabolas: {18}
 - It has a vertex at (4, -3) and passes through (2, -15).
 - It has a y – intercept of -2 and passes through the points (1, 0) and (-2,12).
- (CI) Find the roots of the quadratic equations: {9,10}
 - $f(x) = 2x^2 + 13x + 15$
 - $f(x) = 3x^2 - 11x + 10$
 - $f(x) = 3x^2 - 7x - 6$
- (CI) Solve the quadratic equations: {9,10}
 - $0 = 6x^2 + 23x + 7$
 - $36x^2 = -39x + 35$
- Factor the following quadratic expressions: {7,8}
 - $6x^2 + 11x - 10$
 - $8x^2 - 18x - 5$
 - $9x^2 + 101x + 22$
- Use a GRAPH to help you factor the following quadratic functions. Include an explanation as to WHY and HOW a graph can help you write an equation in factored form. {4,7,8}
 - $2x^2 + 13x + 15$
 - $3x^2 - 11x + 10$
 - $3x^2 - 7x - 6$

6. (CI) Find the roots of $9(x - 3)^2 - 16(x + 1)^2 = 0$ {7,8}

7. Mr. S. is given the equation $\frac{1}{x - 3} + \frac{1}{x + 1} = 1$ and is being asked to solve for x ; {7,8}

a. Graph the system $f(x) = \frac{1}{x - 3} + \frac{1}{x + 1}$ and $g(x) = 1$ and find the intersection point(s).

b. Explain WHY Mr S uses this **system** to solve the original equation.

c. Graph the parabola $k(x) = x^2 - 4x - 1$ and find the zeroes. What do you notice, given your work in the previous parts of this question?

Mr. S now has NO calculator, so must provide an algebra based solution for this problem. He carries out the following steps:

$$\begin{aligned}\frac{1}{x - 3} + \frac{1}{x + 1} &= 1 \\ (x + 1) + (x - 3) &= 1(x - 3)(x + 1) \\ 2x - 2 &= x^2 - 2x - 3 \\ 0 &= x^2 - 4x - 1\end{aligned}$$

d. Explain what Mr. S. did to get the second line of his solution.

e. Given the work & explanations, solve the following:

i. $\frac{1}{x + 3} + \frac{1}{x - 3} = 1$

ii. $\frac{1}{x} + \frac{1}{x + 1} = \frac{5}{6}$



Higher Level Questions for More Complex Concepts OR an EXTENSION of basic concepts involved with Quadratic Functions.

1. Graph the following complex numbers and hence or otherwise, determine $|z|$ for each complex number.
 - a. $z = 3 + 2i$
 - b. $z = -5 + 4i$
 - c. $z = -6 - 3i$
 - d. $z = 2i$
 - e. $z = 5$

2. Show a graphic representation of vector addition wherein you work with $z_1 = 3 + 5i$ and $z_2 = -4 - 2i$.
 - a. Then show the result of $z_1 + z_2$.
 - b. How about vector subtraction \rightarrow try $z_1 - z_2$
 - c. Now try and then $z_2 - z_1$
 - d. What about division and multiplication \rightarrow graph the result.