Lesson 59 - Intermediate Value Theorem

HL Math – Calculus











Example 2

- Determine if f(x) has any real roots, where $f(x) = x^2 - \sqrt{x+1}$ in interval[1,2]
- (1) f(x) is continuous on the interval [1,2]
- (2) f(1) = -ve #
- (3) f(2) = +ve #
 - $\therefore \text{ by IVT } \exists c \in [1,2] \Rightarrow f(c) = 0$

Examples • (3) Is any real number exactly one less than its cube? • (4) Why does the IVT fail to hold for f(x) on [-1, 1]? $f(x) = \begin{cases} -1 & -1 \le x < 0\\ 1 & 0 \le x \le 1 \end{cases}$











f(1)= 1

$$\therefore$$
 by IVT $\exists c \in \left[\frac{1}{2}, 1\right] \ni f(c) = 0$



Example 3

Consider the function ,

$$f(x) = \frac{3}{x+5}$$

- Calculate f(6), f(-5.5), f(0)
- Can you conclude that there must be a zero between f(6) and f(-5.5)?