































## (D) Using the FTA

- Given that 1-3i is a root of  $x^4-4x^3+13x^2-18x-10=0,$  find the remaining roots.
- Write an equation of a third degree polynomial whose given roots are 1 and *i*. Additionally, the polynomial passes through (0,5)
- Write the equation of a quartic wherein you know that one root is 2 i and that the root x = 3 has a multiplicity of 2.

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## (E) Further Examples The equation x<sup>3</sup> - 3x<sup>2</sup> - 10x + 24 = 0 has roots of 2, h, and k. Determine a quadratic equation whose roots are h - k and hk. The 5<sup>th</sup> degree polynomial, f(x), is divisible by x<sup>3</sup> and f(x) - 1 is divisible by (x - 1)<sup>3</sup>. Find f(x). Find the polynomial p(x) with integer coefficients such that one solution of the equation p(x)=0 is 1+√2+√3.

## (E) Further Examples Start with the linear polynomial: y = -3x + 9. The x-coefficient, the root and the intercept are -3, 3 and 9 respectively, and these are in arithmetic progression. Are there any other linear polynomials that enjoy this property? What about quadratic polynomials? That is, if the polynomial y = ax<sup>2</sup> + bx + c has roots r<sub>1</sub> and r<sub>2</sub> can a, r<sub>1</sub>, b, r<sub>2</sub> and c be in arithmetic progression?

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