

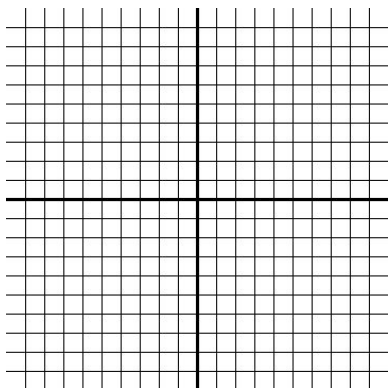
BIG PICTURE of this UNIT:	<ul style="list-style-type: none"> What is a Polynomial and how do they look? What are the attributes of a polynomial? How do I work with polynomials? 		
CONTEXT of this LESSON:	<p>Where we've been</p> <p>We have discussed the basics of polynomial functions (appearance & simple algebra)</p>	<p>Where we are</p> <p>We have solidified the basics of polynomials and their graphs. Now we have a small adventure into rational functions</p>	<p>Where we are heading</p> <p>What are the key attributes of a rational function, linear over linear?</p>

(A) Lesson Objectives:

- Work on and attempt to develop an understanding of KEY rational vocabulary.
- Begin to analyze the the attributes of a rational functions and it's effect on the graph.
- Observations and patterns in the graphs of rational functions.

(B) Review of the rational parent function

Sketch a graph of $y = \frac{1}{x}$. Make sure to include any asymptotes.



Label the TWO key points on this function and write them down:

Write down the equations of the asymptote(s):

State the domain and range:

State the zero(s) (if they exist):

State the extrema (if they exist):

State the intervals of increase and decrease:

Is the function continuous or discontinuous?

(C) Review of transformations

$$f(x) = a(x - c) + d$$

How does “a” affect $f(x)$?

How does “c” affect $f(x)$?

How does “d” affect $f(x)$?

(D) Rational Functions Investigation #1

Using Desmos and your brain, let's explore rational functions! Open this Google Doc, make a copy for you and your partner, and then fill out the table in the document investigating $f(x) = \frac{1}{x - c} + d$.

(E) Rational Functions Investigation #2

Using Desmos and your brain, let's explore rational functions! Using the same Google Doc, fill out the table in the document investigating $f(x) = \frac{a}{x}$ and $f(x) = \frac{a}{x - c} + d$.

Transformation form for rational functions: $f(x) = \frac{a}{x - c} + d$

EVENTUALLY, we will look at rational functions taking the form below. In this course $g(x)$ and $h(x)$ will be restricted to linear functions of the form $ax + b$. So we will be working with functions that look a bit like...

$$f(x) = \frac{g(x)}{h(x)} = \frac{ax + b}{cx + d}$$

ex.

$$f(x) = \frac{2x - 1}{x + 5}$$

*It is a much needed fact that $h(x) \neq 0$.

(F) Algebra with Rational Functions

Converting from transformation form to linear/linear.

Write the following as ONE fraction:

$$\frac{2}{x} + 3$$

$$4 - \frac{3}{x}$$

$$\frac{1}{x + 3} + 1$$

$$\frac{1}{x - 2} - 4$$

$$\frac{1}{x + 5} - 2$$

$$\frac{1}{x - 4} + 3$$