

### PLANES

Although a line in space is determined by a point and a direction, a plane in space is more difficult to describe.

• A single vector parallel to a plane is not enough to convey the 'direction' of the plane.







### Example 1

• Determine the vector and parametric equations of the plane that contains the points A(1,0,-3), B(2,-3,1) and C(3,5,-3)

Example 2

• Does the point (4,5,-3) lie in the plane

# $\vec{r} = (4,1,6) + t(3,-2,1) + \lambda(-6,6,-1)$

# A











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The normal vector **n** is orthogonal to every vector in the given plane.

In particular, **n** is orthogonal to  $\mathbf{r} - \mathbf{r}_0$ .

Thus, we have:  $\mathbf{n} \cdot (\mathbf{r} - \mathbf{r}_0) = 0$ 

That can also be written as:  $\mathbf{n} \cdot \mathbf{r} = \mathbf{n} \cdot \mathbf{r}_0$ 



































## Example 4:

Given the normal vector, <3, 1, -2> to the plane containing the point (2, 3, -1), write the equation of the plane in both standard form and general form.

Solution:

al vector, <3, 1, -2> to the plane containing -1), write the equation of the plane in both and general form.
$a(x - x_0) + b(y - y_0) + c(z - z_0) = 0$
3(x-2)+1(y-3)-2(z+1)=0
3x - 6 + y - 3 - 2z - 2 = 0
or
3x + y - 2z - 11 = 0







