

Lesson 7: Graphs of Exponential Relations | Unit 4 – Exponential Relations

(A) Lesson Context

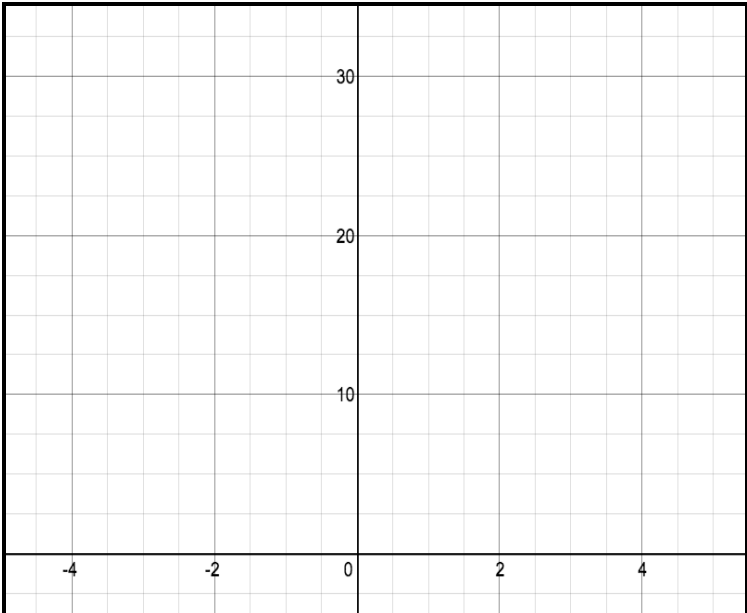
BIG PICTURE of this UNIT:	<ul style="list-style-type: none"> How can I analyze growth or decay patterns in data sets & contextual problems? How can I algebraically & graphically summarize growth or decay patterns? How can I compare & contrast linear and exponential models for growth and decay problems. 		
CONTEXT of this LESSON:	Where we've been In Lessons 5 & 6, you looked at how exponential equations can be used to model real world scenarios	Where we are How do we interpret and analyze graphs of exponential equations that model growth & decay patterns	Where we are heading How can I use graphs & equations that will help me make predictions about scenarios which feature exponential growth & decay?

(A) Lesson Objectives:

- Understand the basic appearance and features of the graph of a simple exponential relation
- Make predictions/extrapolations through graphic analysis
- Understand the basic connection between the parameters in an equation and its appearance in a graph

(B) Graphs of Exponential Functions – Investigation #1- The BASIC graph of $y = Ca^x$

- Use your TI-84 (or use DESMOS) to graph the equation $y = 2^x$. Then sketch the graph on the attached grid. Fill in the included data table as well.

GRAPH: 	DATA TABLE: <table border="1" style="width: 100%; text-align: center;"> <tr> <td>X</td><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td> </tr> <tr> <td>Y</td><td></td><td></td><td></td><td></td><td></td><td></td> </tr> </table> <table border="1" style="width: 100%; text-align: center;"> <tr> <td>X</td><td>-1</td><td>-2</td><td>-3</td><td>-4</td><td>-5</td> </tr> <tr> <td>Y</td><td></td><td></td><td></td><td></td><td></td> </tr> </table>	X	0	1	2	3	4	5	Y							X	-1	-2	-3	-4	-5	Y					
X	0	1	2	3	4	5																					
Y																											
X	-1	-2	-3	-4	-5																						
Y																											
Domain → Range →	y-intercept → asymptote →																										

Lesson 7: Graphs of Exponential Relations | Unit 4 – Exponential Relations

(C) Graphs of Exponential Functions – Investigation #2 – Changing the value of C in $y = Ca^x$

- a. Use your TI-84 (or use DESMOS) to graph the equation $y = 2^x$. Then on the same graph, graph the following equations in order to compare the appearance of the graphs & compare the data points.

Equation to graph	Sketch	Compare the two graphs	Compare the two data tables
$Y = 2(2)^x$			
$Y = 10(2)^x$			
$Y = 0.5(2)^x$			
$Y = 0.1(2)^x$			
Describe the effect of changing the value of C in the equation $y = Ca^x$.			

Lesson 7: Graphs of Exponential Relations | Unit 4 – Exponential Relations

(D) Graphs of Exponential Functions – Investigation #3 – Changing the value of a in $y = Ca^x$

- a. Use your TI-84 (or use DESMOS) to graph the equation $y = 2^x$. Then on the same graph, graph the following equations in order to compare the appearance of the graphs & compare the data points.

Equation to graph	Compare the two graphs	Compare the two data tables
$Y = (3)^x$		
$Y = (5)^x$		
$Y = (\frac{1}{2})^x$		
$Y = (\frac{1}{4})^x$		

Describe the effect of changing the value of a in the equation $y = Ca^x$.

Lesson 7: Graphs of Exponential Relations | Unit 4 – Exponential Relations

(E) Graphs of Exponential Functions – Investigation #4 – Changing the signs in $y = Ca^x$

- a. Use your TI-84 (or use DESMOS) to graph the equation $y = 2^x$. Then on the same graph, graph the following equations in order to compare the appearance of the graphs & compare the data points.

Equation to graph	Compare the two graphs	Compare the two data tables
$Y = -(2)^x$		
$Y = (2)^{-x}$		
$Y = (-2)^x$		
Describe the effect of changing the signs in the equation $y = Ca^x$.		

Lesson 7: Graphs of Exponential Relations | Unit 4 – Exponential Relations

(F) Graphs of Exponential Functions – Investigation #5 – Introducing a shift in $y = Ca^x$

- a. Use your TI-84 (or use DESMOS) to graph the equation $y = 2^x$. Then on the same graph, graph the following equations in order to compare the appearance of the graphs & compare the data points.

Equation to graph	Compare the two graphs	Compare the two data tables
$Y = (2)^x + 3$		
$Y = (2)^x + 8$		
$Y = (2)^x - 3$		
$Y = (2)^x - 7$		
Describe the effect of adding/subtracting another value in the equation $y = Ca^x + D$		

(G) Consolidation of Concepts

Without a graphing calculator, use your understanding of the concepts that you learned in order to prepare a (i) data table and a (ii) graph of the following equations:

$Y = -(2)^x + 5$	$Y = -4 + \frac{1}{2}(2)^{-x}$