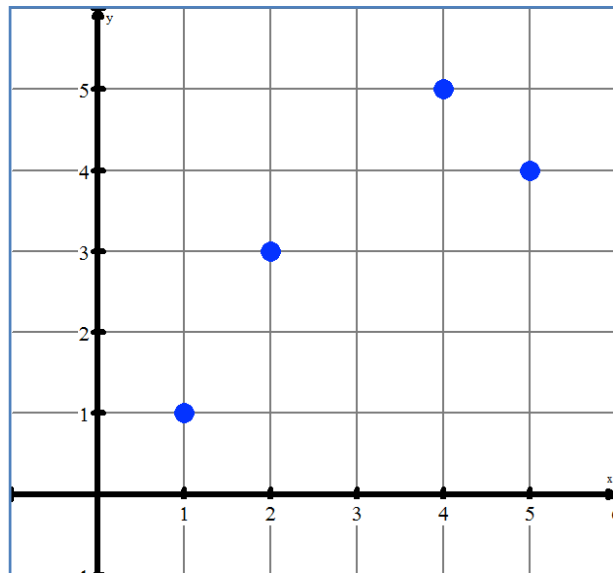


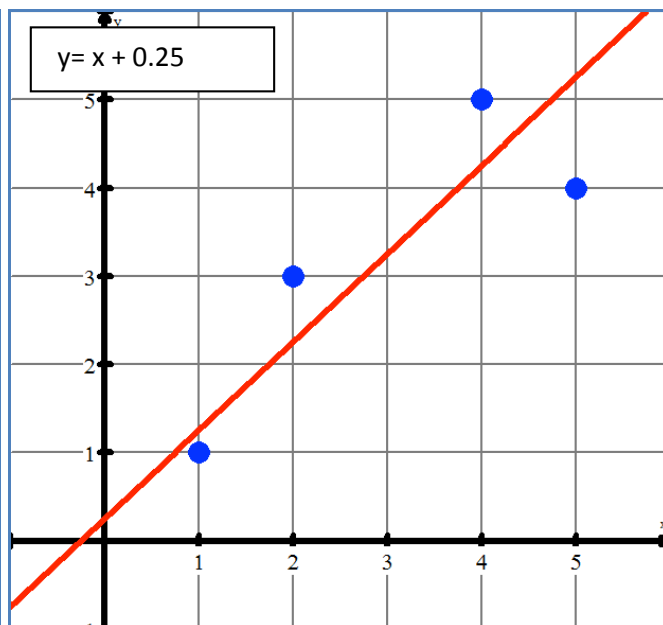
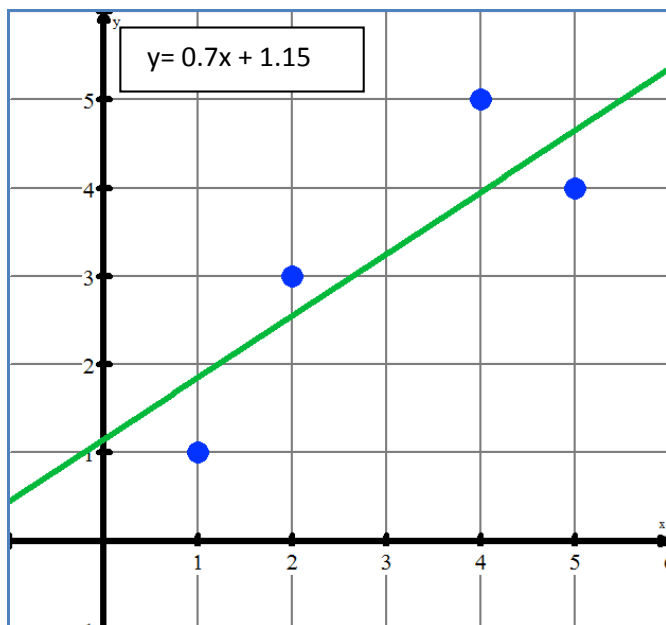
Working with the Least Squares Regression Line | Lesson 68

(A) **EXPLORATION #1** → Data Set #1 → (1,1); (2,3); (4,5); (5,4)

- Calculate the mean point
- Draw the line of best fit AS YOU PERCEIVE IT!!!
- Determine the equation of the line you drew.



- Student #1 drew the LoBF & decides that the line of best fit has an equation of $y = 0.7x + 1.15$. But Student #2 drew the LoBF & decides that the equation of the the line should be $y = x + \frac{1}{4}$. (see graph #2 & graph #3)



- Q → Is there some way descriptive way we can determine whose line is a “better” fit for the data?
- Q → Is there some analytical/numeric way we can determine whose line is a “better” fit for the data?

(B) Calculating “Residuals”

a. Working With Student # _____. and the equation $f(x) =$ _____.

x	y	f(x) =	Residual = y – f(x)	Square of residual
1	1			
2	3			
4	5			
5	4			
$\bar{x} =$	$\bar{y} =$			Σ

b. Working With Student # _____. and the equation $f(x) =$ _____.

x	y	f(x) =	Residual = y – f(x)	Square of residual
1	1			
2	3			
4	5			
5	4			
$\bar{x} =$	$\bar{y} =$			Σ

c. CONCLUSION → Which line “fits” better? Why?

d. Now let’s go to the following animation and “play” with a line of best fit on a data set: at <http://hspm.sph.sc.edu/courses/J716/demos/LeastSquares/LeastSquaresDemo.html>

Closing Question → How do I determine which line minimizes the squares of the residuals???

(C) Determining the Eqn of the Least Squares Regression Line & Regression Coefficient

Recall some of our formulas from Lesson 67:

$$s_{xy} = \frac{\sum(x - \bar{x})(y - \bar{y})}{n} = \frac{\sum xy}{n} - \bar{x}\bar{y} \quad \text{and} \quad s_x = \sqrt{\frac{\sum(x - \bar{x})^2}{n}} = \sqrt{\frac{\sum x^2}{n} - \bar{x}^2} \quad \text{and}$$

$$s_y = \sqrt{\frac{\sum(y - \bar{y})^2}{n}} = \sqrt{\frac{\sum y^2}{n} - \bar{y}^2} \quad \text{and} \quad r = \frac{s_{xy}}{s_x s_y} \quad \text{as well as other formulas for } r \rightarrow$$

$$r = \frac{\sum xy - \frac{\sum x \sum y}{n}}{\sqrt{\sum x^2 - \frac{(\sum x)^2}{n}} \sqrt{\sum y^2 - \frac{(\sum y)^2}{n}}} = \frac{\sum(x - \bar{x})(y - \bar{y})}{\sqrt{\sum(x - \bar{x})^2} \sqrt{\sum(y - \bar{y})^2}} = \frac{\sum xy - n\bar{x}\bar{y}}{\sqrt{\sum x^2 - n\bar{x}^2} \sqrt{\sum y^2 - n\bar{y}^2}}$$

so let's apply these calculations here:

x ²	X	y	y ²	xy
	1	1		
	2	3		
	4	5		
	5	4		
Σ	Σ so $\bar{x} =$	Σ so $\bar{y} =$	Σ	Σ

So then $s_x =$ _____, $s_y =$ _____, $s_{xy} =$ _____, and $r =$ _____.

Then we add one more formula that will help us write an equation of the least square regression line \rightarrow

$$y - \bar{y} = \frac{s_{xy}}{(s_x)^2} (x - \bar{x}) \rightarrow \text{so our equation in our example should be } \rightarrow$$

Now test it out on the TI-84 \rightarrow

(D) Further Examples → HH Textbook 18C, p589, Q3

Data Set:

Spray Concentration (mL/L)	3	5	6	8	9	11
Yield of Tomatoes (per bush)	67	90	103	120	124	150

x ²	x	y	y ²	xy
	3	67		
	5	90		
	6	103		
	8	120		
	9	124		
	11	150		
Σ	Σ so $\bar{x} =$	Σ so $\bar{y} =$	Σ	Σ

So then $s_x =$ _____, $s_y =$ _____, $s_{xy} =$ _____, and $r =$ _____.

the least square regression line → $y - \bar{y} = \frac{s_{xy}}{(s_x)^2} (x - \bar{x})$ → so our equation in our example should be →

(E) Further Examples → HH Textbook 18C, p589, Q5

Data Set:

Frost Free days	75	100	125	150	175	200
Rate of Reaction	44.6	42.1	39.4	37.0	34.1	31.2

x ²	x	y	y ²	xy
	75	44.6		
	100	42.1		
	125	39.4		
	150	37		
	175	34.1		
	200	31.2		
Σ	Σ so $\bar{x} =$	Σ so $\bar{y} =$	Σ	Σ

So then $s_x =$ _____, $s_y =$ _____, $s_{xy} =$ _____, and $r =$ _____.

the least square regression line → $y - \bar{y} = \frac{s_{xy}}{(s_x)^2} (x - \bar{x})$ → so our equation in our example should be →

Now test it out on the TI-84 →