

(A) Lesson Objectives:

- a. Introduce arithmetic series through an investigation.
- b. Introduce the formulas associated with arithmetic series.
- c. Apply arithmetic series to real world scenarios.

(B) Definitions:

- a. A **SERIES** simply refers to the sum of the terms of a sequence
- b. Mathematically, $S_n = u_1 + u_2 + u_3 + \dots + u_{n-1} + u_n$

(C) Exploring Patterns and Series

- a. Let's work with PARTIAL SUMS to find some patterns and strategies for finding sums (NO CALCULATORS ALLOWED)
 - i. The sum of the first 10 natural numbers is:
 - ii. The sum of the first 20 natural numbers is:
 - iii. The sum of the first 30 natural numbers is:
 - iv. So the sum of the first 100 natural numbers is:
- b. Work out the sum of the first 50 positive even integers.
- c. Work out the sum of all the odd numbers from 21 up to 99.

(D) Key Ideas – Formula for Arithmetic Series

- a. The formula for the sum of an arithmetic series is:

(E) Examples:

ex 1. For the series $2 + 11 + 20 + 29 + \dots$, find u_{20} and S_{20}

ex 2. Find the sum of the first 30 terms of the series $11 + 6 + 1 - 4 - 9 \dots$

ex 3. Jayne buys 10 widgets on the Jan 1st, 15 on the 1st of Feb, 20 on the 1st of March, etc..... How many widgets has she acquired in 2 years?

ex 4. Determine the sum of the series $12 + 23 + 34 + 45 + \dots + 364$

ex 5. A sequence is defined by the terms $2, 5, 8, 11, 14, 17, \dots$ find the sum of the series starting with the 11th term and ending with the 28th term.

ex 6. Shayla deposits \$128 into her account. Each week she deposits \$7 less than the previous week until she deposits her last deposit of \$2. What total amount did she deposit?

(F) Homework/Resources

- **HW: from HH Textbook** → HH Textbook, Exercise 12G.1, p412, Q1abe as well as Exercise 12G.2, p413, Q2ad, 3ac, 4, 6, 7, 10, 11
- Video Help: <http://www.youtube.com/watch?v=UHkueFmPC6s>