Lesson 25 – Applications of Exponential & Logarithmic Functions

IB Math SL1 - Santowski

Example 1

11/18/2010

11/18/2010

 Mr. S. drinks a cup of coffee at 9:45 am and his coffee contains 150 mg of caffeine. Since the half-life of caffeine for an average adult is 5.5 hours, determine how much caffeine is in Mr. S.'s body at class-time (1:10pm). Then determine how much time passes before I have 30 mg of caffeine in my body.

Math SL1 - Santowsk

Example 2

11/18/2010

• Two populations of bacteria are growing at different rates. Their populations at time *t* are given by $P_1(t) = P_0 5^{t+2}$ and $P_2(t) = P_0 e^{2t}$ respectively.

Math SL1 - Santowsk

- At what time are the populations the same?
- $\hfill\square$ When is the population of P_2 twice that of $P_1?$

Math SL1 - Santowsk

Example 4

11/18/2010

11/18/2010

- You invest \$5000 in a stock that grows at a rate of 12% per annum compounded quarterly. The value of the stock is given by the equation V = 5000(1 + 0.12/4)^{4x}, or V = 5000(1.03)^{4x} where x is measured in years.
 - Find the value of the stock in 6 years.
 - Find when the stock value is \$14,000

Math SL1 - Santowski

Example 3 Dry cleaners use a cleaning fluid that is purified by evaporation and condensation after each cleaning cycle. Every time it is purified, 2% of the fluid is lost An equipment manufacturer claims that after 20 cycles, about two-thirds of the fluid remains. Verify or reject this claim. If the fluid has to be "topped up" when half the original amount remains, after how many cycles should the fluid be topped up? A manufacturer has developed a new process such that two-thirds of the cleaning fluid remains after 40 cycles.

What percentage of fluid is lost after each cycle?

Math SL1 - Santowski

Example 5 The population of a small town was 35,000 in 1980 and in 1990, it was 57,010. Create an algebraic model for the towns population growth. Check your model using the fact that the population was 72800 in 1995. What will the population be in 2010? When will the population be 100,000?

Example 6

11/18/2010

- The sales S (in thousands of units) of a new CD burner after it has been on the market for *t* years are given by S(t) = 100(1 - e^{kt}). Fifteen thousand units of the new product were sold the first year.
 - Complete the model by solving for k.
 - Use your calculator to graph the model.

Math SL1 - Santowsk

- Determine S(3) and interpret.
- When were 8,000 units sold?









