

## Physics Class Work – Friction Problems

### Example

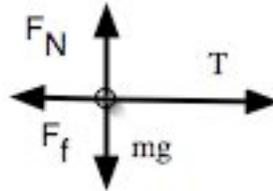
Coefficient of friction can be determined from the force required to drag an object at constant speed, and the weight of the object. A 49-N block is pulled by a horizontal force of 50.0 N along a rough horizontal surface at a constant acceleration of 6 m/s/s. What is the coefficient of friction?



Answer to example 4:

$$\begin{aligned} F_g &= 49\text{-N} \\ T &= 50.0\text{ N} \\ a &= 6\text{ m/s/s.} \\ \mu &= ? \end{aligned}$$

Free-body diagram:



This free body diagram shows normal force cancelling weight, and friction partially offsetting tension or applied force.

Sum the forces: In the vertical axes forces are equal and opposite as there is no vertical acceleration.

$$\begin{aligned} F_N &= -F_g \\ F_N &= mg = 49\text{ N} \end{aligned}$$

$$\text{Also, } m = 49/9.81 = 4.99\text{ kg}$$

In the horizontal axis,

$$\begin{aligned} F_{\text{net}} &= T + F_f \\ F_{\text{net}} &= (50\text{ N}) + F_f \end{aligned}$$

Newton's Second Law:

$$F_{\text{net}} = ma$$

$$F_{\text{net}} = (4.99\text{ kg})(6) = 30.0\text{ N}$$

$$\text{Therefore, } F_f = F_{\text{net}} - T = 30.0\text{ N} - 50.0\text{ N} = -20.0\text{ N (directed against the motion)}$$

$$\text{Thus } \mu = F_f/F_N = 20.0\text{N}/49.0\text{N} = 0.408$$

### Problems

1. A 15.0 kg block is pulled by a horizontal force of 30.0 N along a rough horizontal surface at constant velocity. What is the coefficient of friction?

Tension on a string pulls a block along a horizontal surface.

2. A car is traveling at 60.6 mph on a horizontal highway. The acceleration of gravity is 9.8 m/s<sup>2</sup>. If the coefficient of friction between road and tires on a rainy day is 0.056, what is the minimum distance in which the car will stop? Answer in units of m.

3. If the coefficient of kinetic friction between a 35 kg crate and the floor is .30, what horizontal force is required to move the crate at a steady speed across the floor? What horizontal force is required if  $\mu_k$  is zero?
4. A 300 lbs car is loose inside a shopping mall where  $\mu_k=0.5$ . If the car is initially traveling at 60 f/sec.  
a) what is the kinetic friction force, if the brakes are locked?  
b) what distance will it take to stop if the brakes are locked?
5. Car A is towing car B. Both cars have the same mass  $m_a = m_b = 1000$  kg. Car A has four-wheel drive, and the static coefficient of friction between its tires and the road is  $\mu_s = 1.00$ . Neglect any friction force acting on car B. Car A is accelerating at 1m/s/s. Calculate the tension in the horizontal rope connecting the cars.
6. A 4.0 kg toboggan rests on a frictionless icy surface and a 2.0 kg box rests on top of the toboggan. The coefficient of static friction between the box and toboggan is .60, whereas kinetic friction coefficient is .51. The box is pulled by a 30 N force along the horizontal parallel to the icy floor. What are the magnitudes and directions of the resulting accelerations of the block and toboggan?
7. Four blocks are arranged on a frictionless surface. Two smaller placed on two larger, and a cord connects the two top (small) blocks, and a cord is used to pull the first large block. There is friction only between the top and bottom blocks. What is the maximum value of  $F$  applied to one of the blocks to make all four move with the same acceleration?
8. A block of mass 1.95 kg slides with an initial speed of 4.33 m/s on a smooth, horizontal surface. The block now encounters a rough patch with a coefficient of kinetic friction given by  $\mu_k = 0.260$ . What is the acceleration of the block when it is in the rough patch?
9. A packing crate is placed on a plane inclined at an angle of  $35^\circ$  from horizontal. If the coefficient of static friction between the crate and the plane is 0.65, will the crate slide down the plane?
10. Suppose that you are standing on a train accelerating at  $0.10g$ . What minimum coefficient of static friction must exist between your feet and the floor if you are not to slide?
11. In attempting to move a heavy couch (mass 200 kg) across a rug-covered floor, a man finds he must exert a horizontal force of 700 N to get the couch to barely move. Once the couch starts moving, the man continues to push with 700 N and his daughter, a physics major, estimates that it then accelerates at  $1.10$  m/s<sup>2</sup>. Determine (a) the coefficient of static friction and (b) the coefficient of kinetic friction between the couch and the rug.
12. A 2500kg car traveling 14.0 m/s on an icy, level road approaches an intersection. The brakes lock and the car skids 25.0m. What is the coefficient of friction between the tires and the surface?
13. A 10,000-kg load sits on the flat bed of a 20,000-kg truck moving at 12.0 m/sec. The load is not tied down to the truck and has a coefficient of static friction of 0.500 with the truck bed. Calculate the minimum stopping distance for which the load will not slide forward relative to the truck.